



# Mobile-Assisted Localization in Wireless Sensor Networks

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2006/01/13

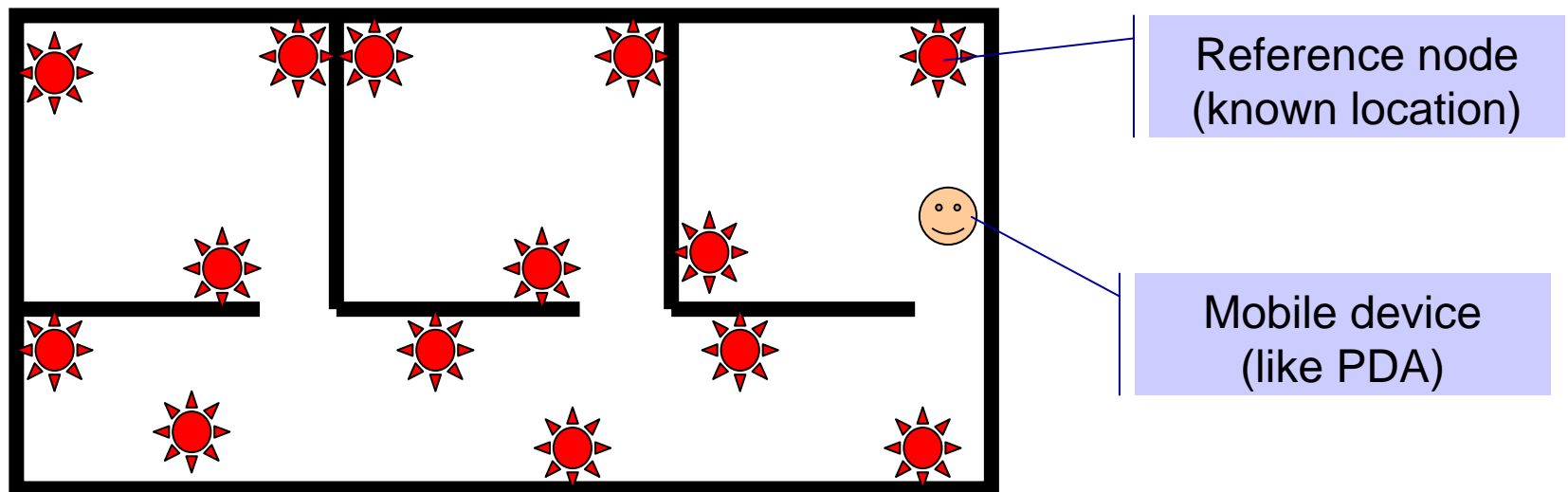


# Outline

- Introduction
- MAL: Mobile-Assisted Localization
  - Distance Measurement
  - Movement strategy
- AFL: Anchor-free Localization
  - Proposed in 2003 April
- Simulation
- Conclusion

# Introduction

- Knowledge of sensor location enable
  1. Sensed data useful to application
  2. Efficient routing protocol
- Node location information is also useful in indoor environment



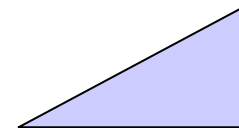
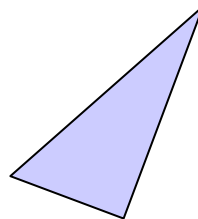
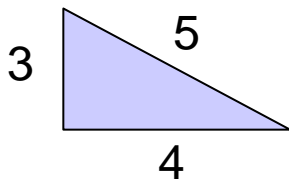
# Introduction



- How reference node know location
  - Manually configuring
    - Cumbersome and error-prone
  - Automatically localize
    - Each node obtain distance to neighbor
    - Computes a coordinate assignment for all node

# Introduction

- The **localization problem** is to determine an assignment of coordinates to nodes in a wireless ad-hoc or sensor network that is consistent with measured pairwise node distances.
- In the absence of an external coordinate reference, this assignment can be unique only up to an arbitrary **rotation**, **translation**, and possible **reflection**, but its scale is determined by the measured ranges.



# Introduction

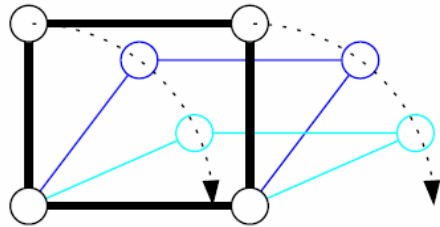


- This paper shows that use the mobile device to measure pairwise node distance
  - Then fed the distance information into AFL
- Why do we use the mobile device ?

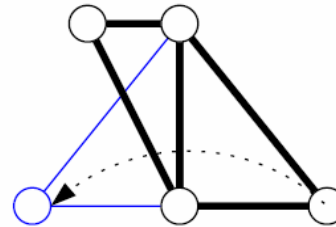
# Indoor Localization Problems

● Obs

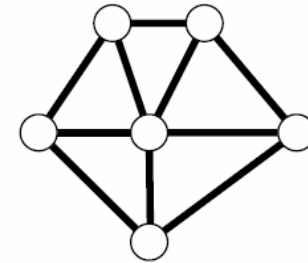
○ E  
ins



not locally rigid



locally rigid  
not globally rigid



globally rigid

placed

● The

dware

A framework that can be continuously deformed while still satisfying all the constraints is said to be *flexible*; otherwise it is *rigid*.

A graph is **globally rigid** if it has a unique embedding



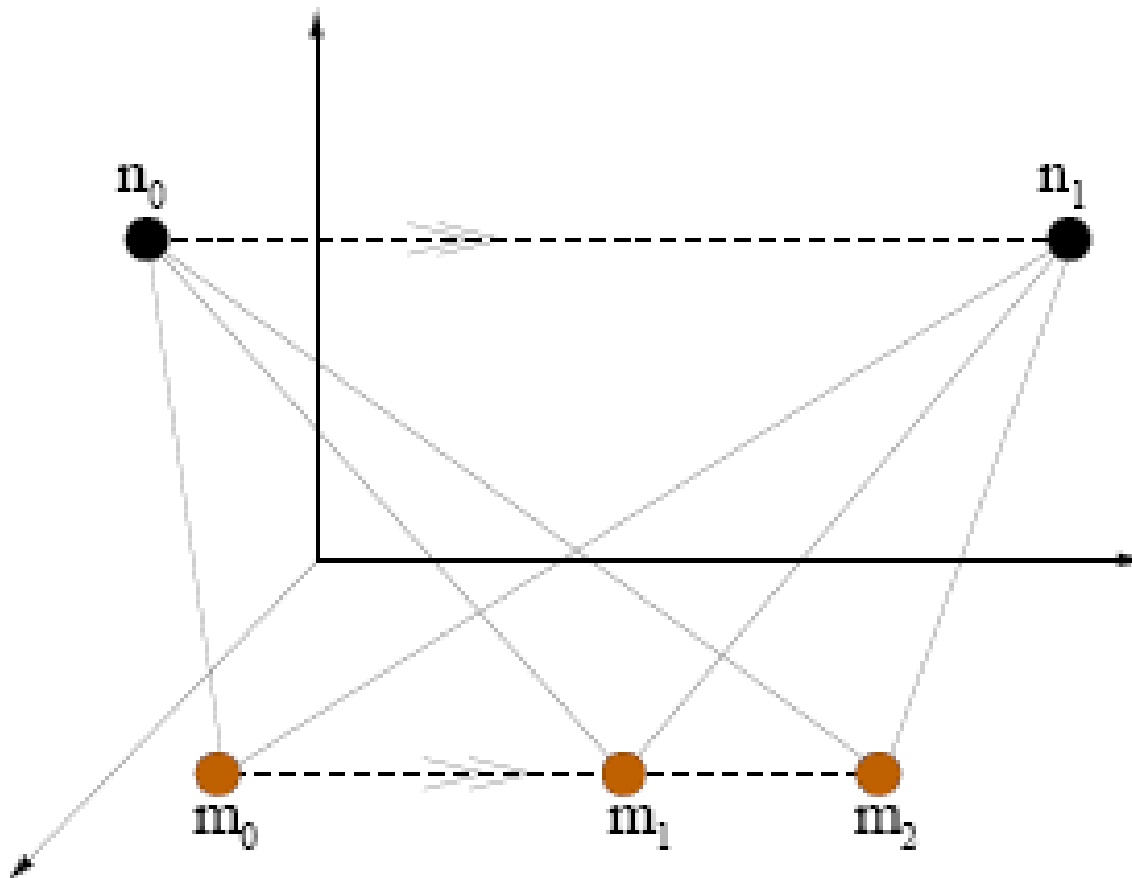
MAL:

three distance measurement approach

1. Measure distance between **two** node at a time
2. Measure distance between **three** nodes at a time
3. Measure distance between **four or more** nodes at a time



# Measure distances among **two** nodes



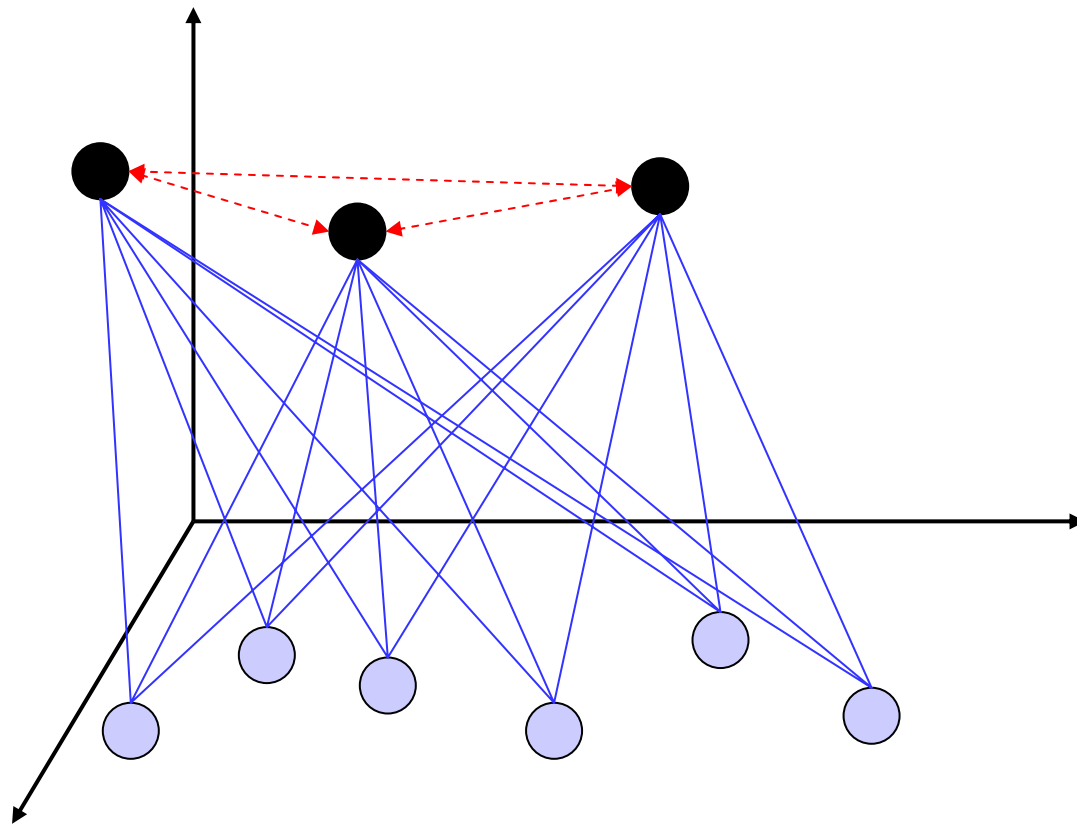
**Assumption:**  
At least need 3  
mobile position

$n_0, n_1, m_0, m_1, m_2$   
are coplanar

$m_0, m_1, m_2$  are  
collinear

Use a larger  
number of points  
would reduce  
GDOP

# Measure distances among **three** nodes



**Assumption:**

At least need **6** mobile position

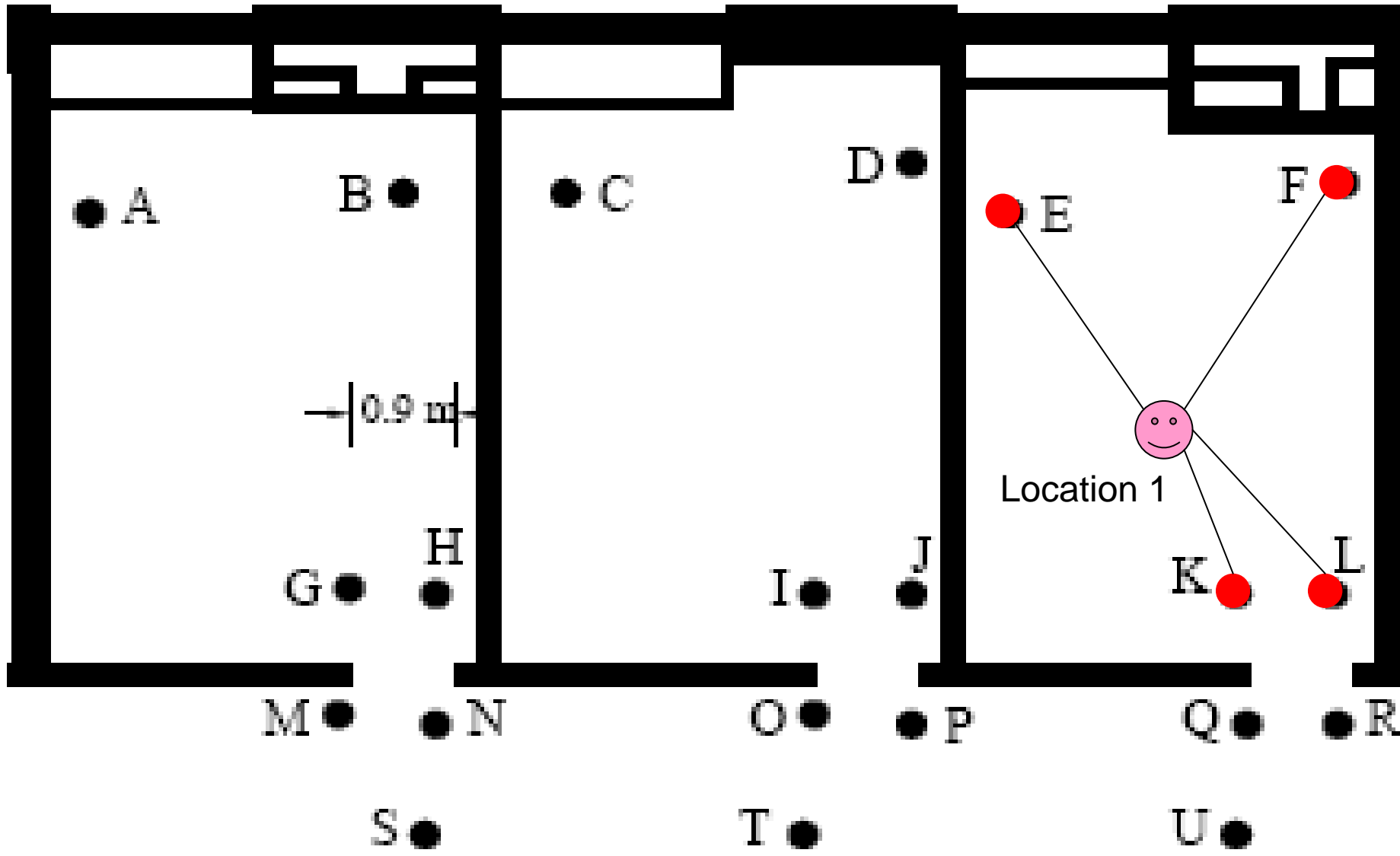
$n_0, n_1, n_2$  are **non-collinear**

$m_0 \sim m_5$  are **coplanar** no **three** of which are **collinear**

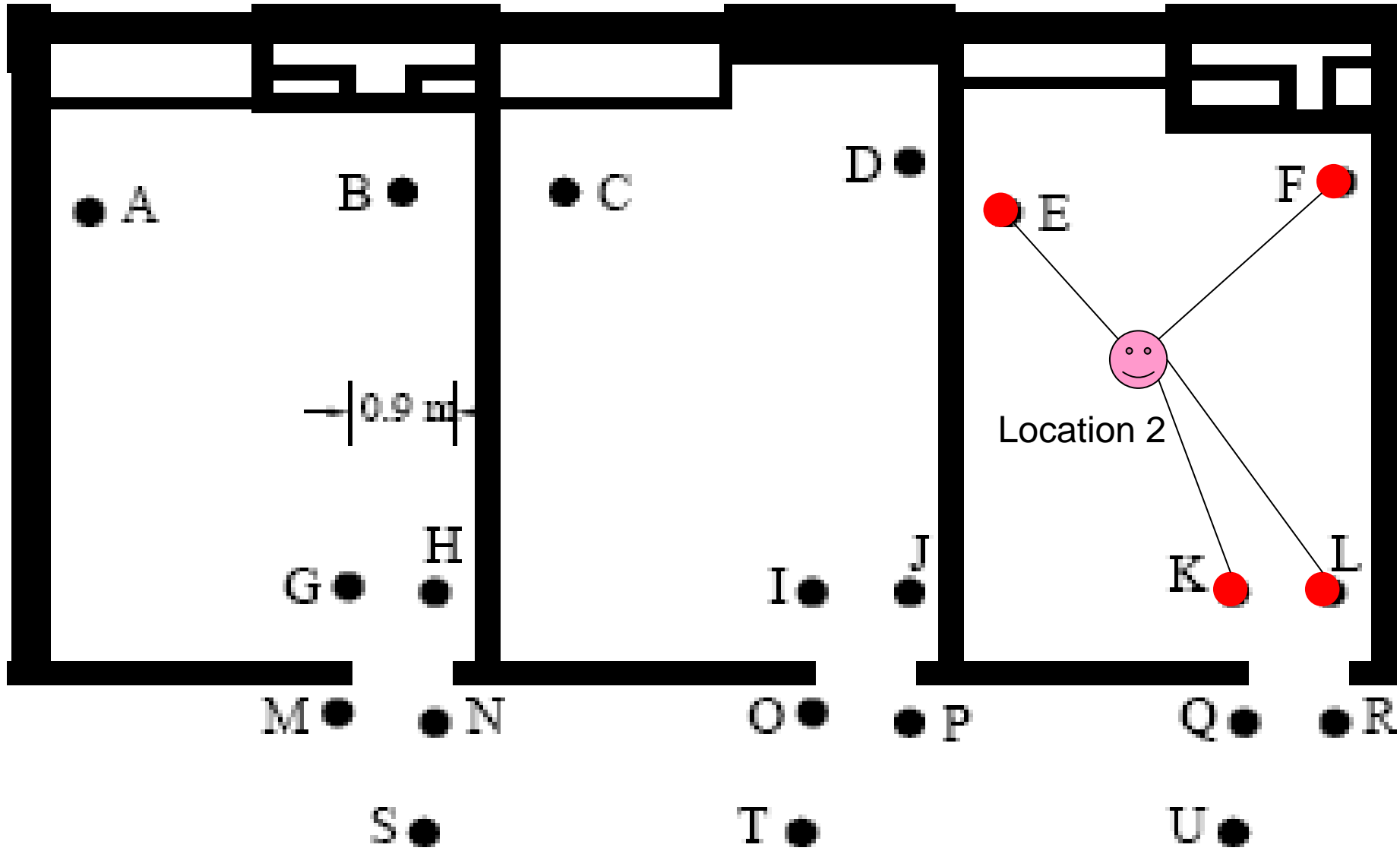
# Measure distances among **four or more** nodes

- Require at least  $\lceil (3j-5)/(j-3) \rceil$  mobile position
- Ex.  $J=4$  then  $\lceil (3j-5)/(j-3) \rceil = 7$ 
  - At least need 7 mobile position
- Assumption
  - $n_1, n_2, n_3, n_4, m_1, m_2, m_3, m_4, m_5, m_6, m_7$
  - No four of which are coplanar

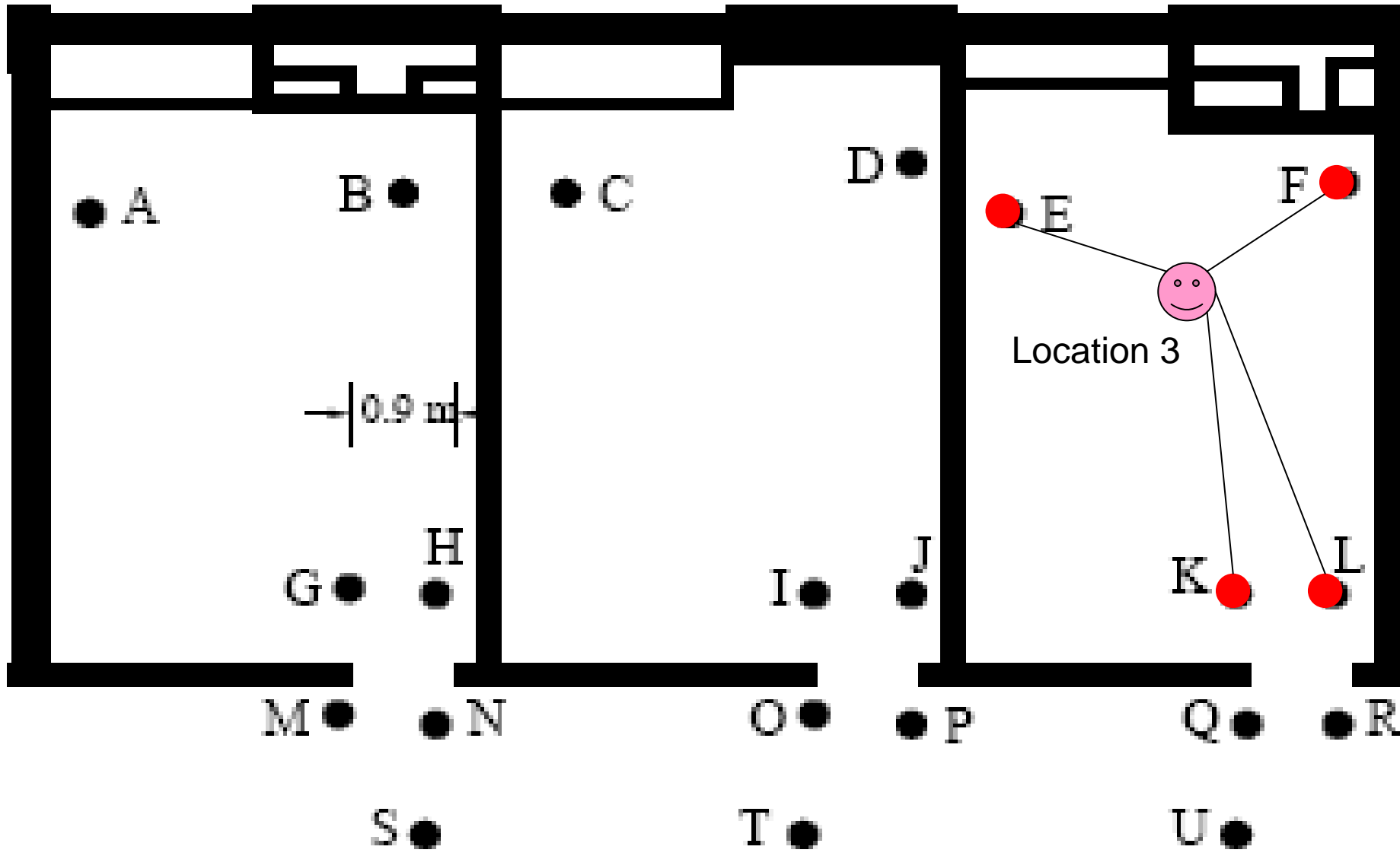
# Movement Strategy: Initialize



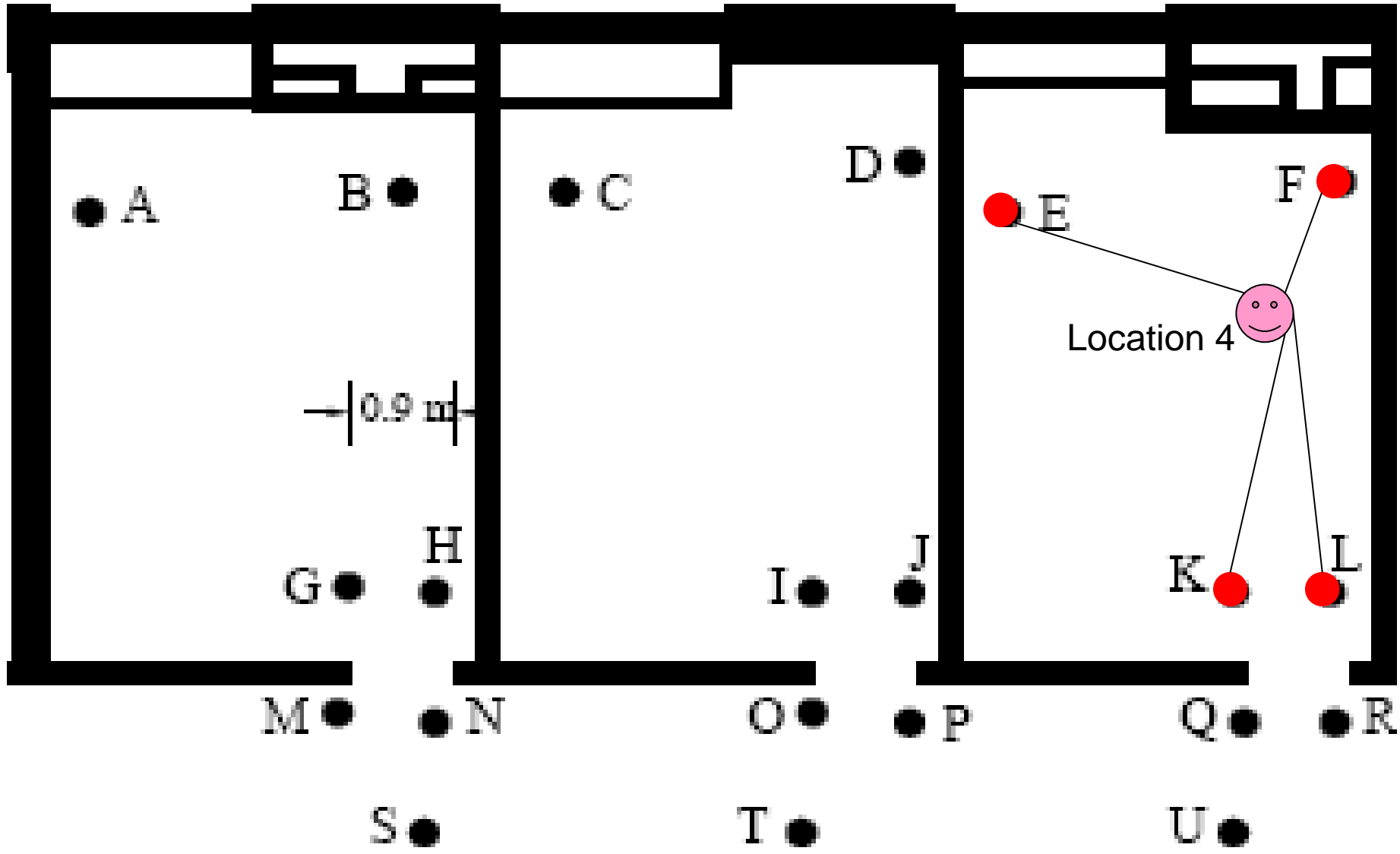
# Movement Strategy: Initialize



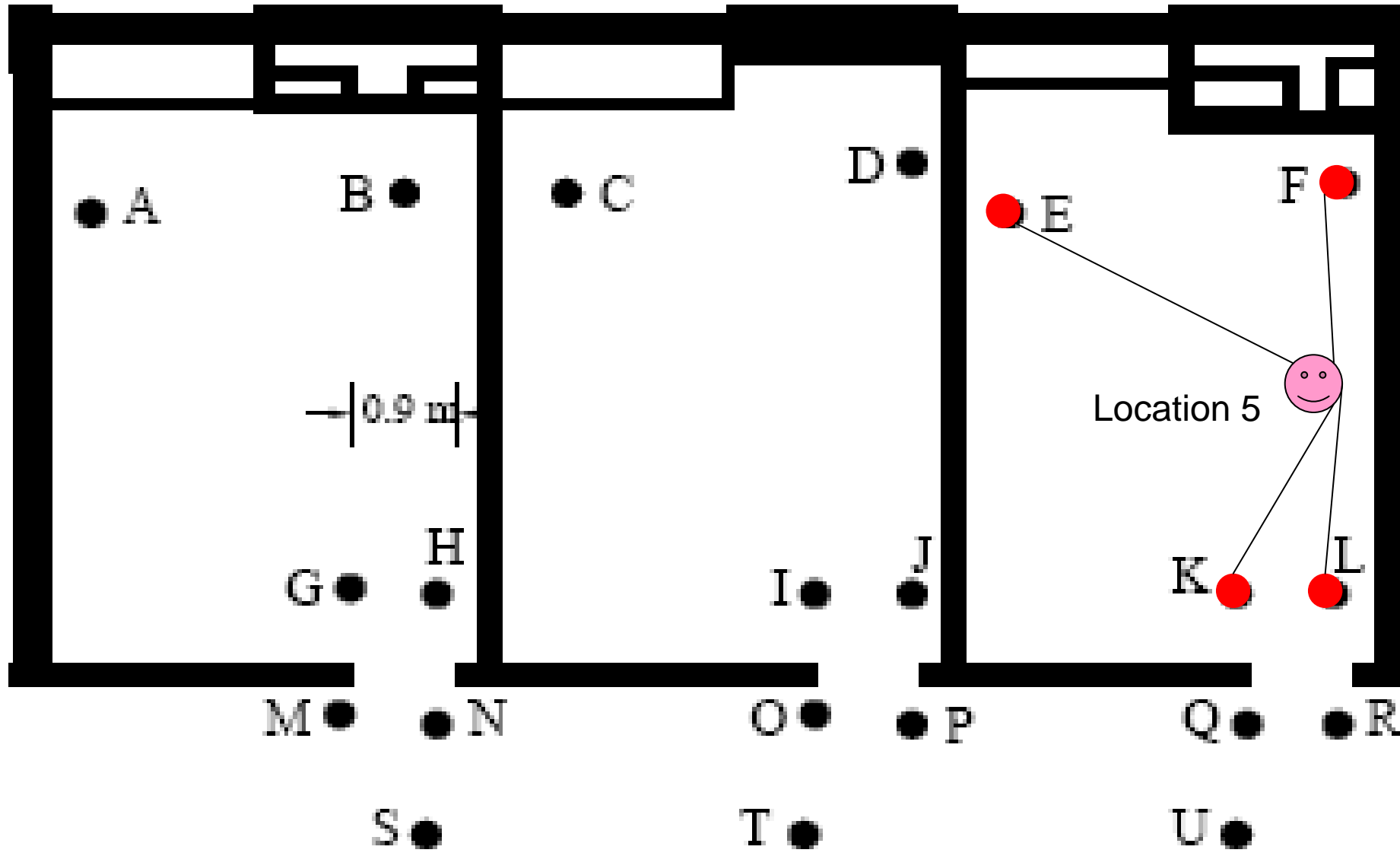
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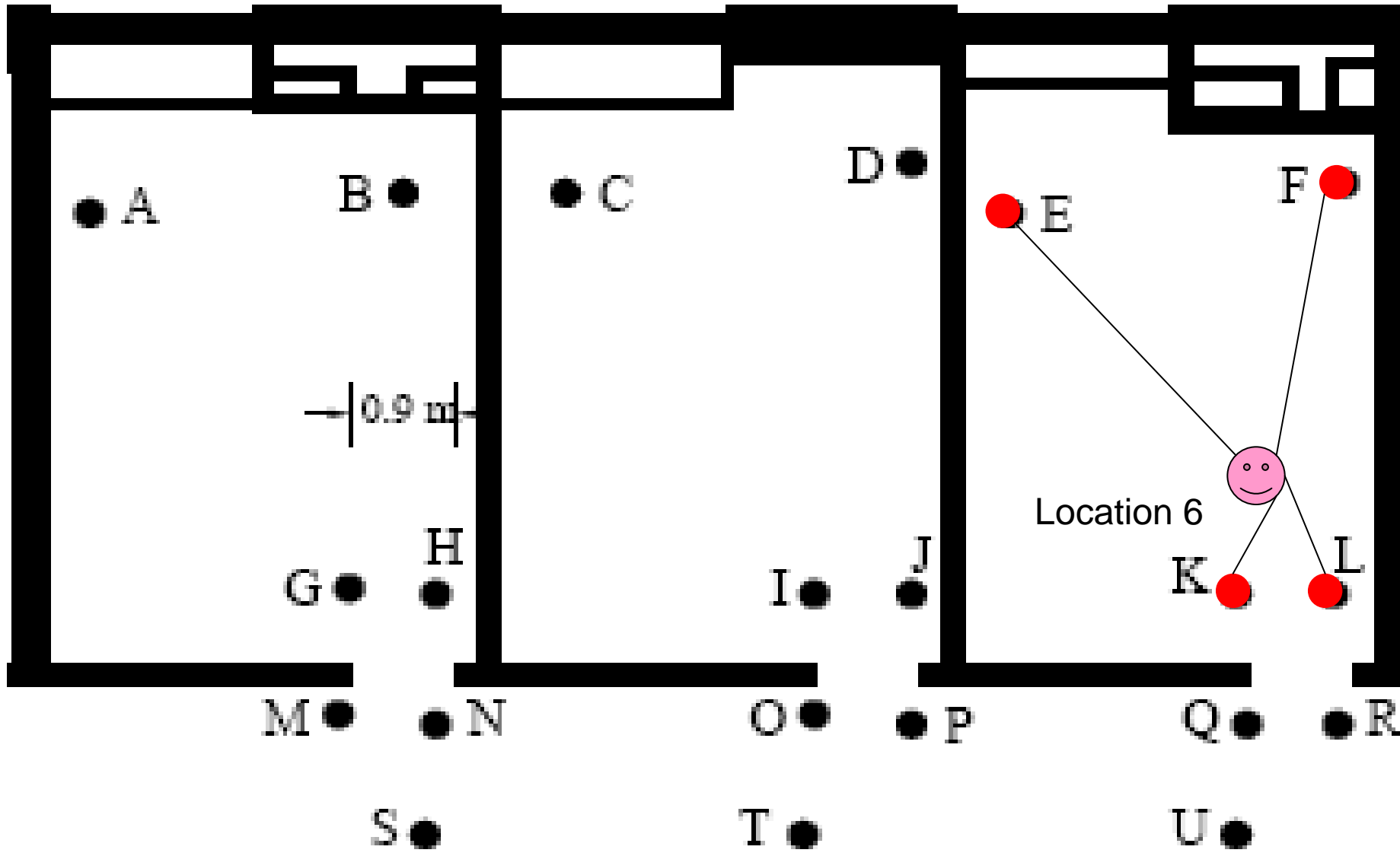


# Movement Strategy: Initialize

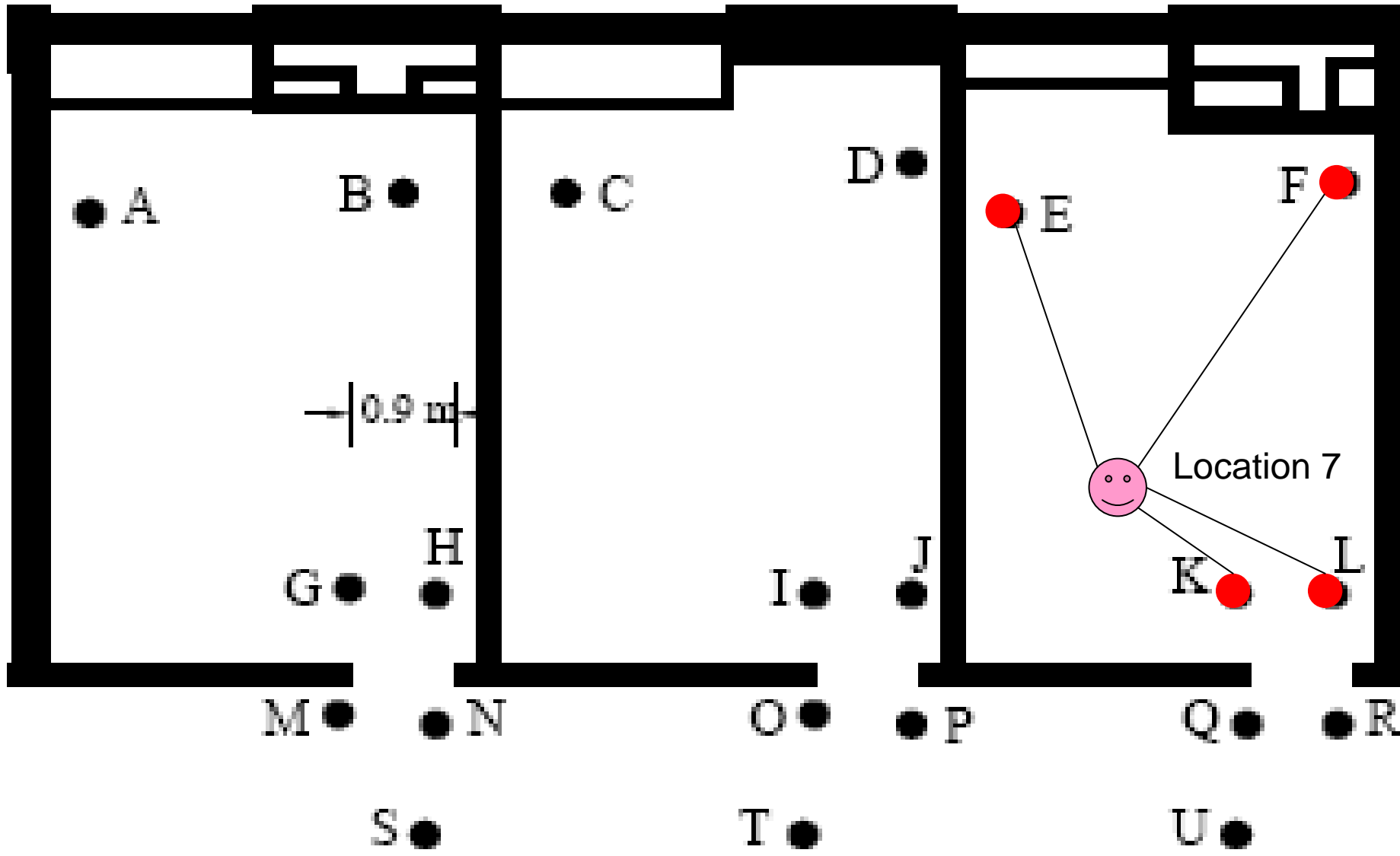




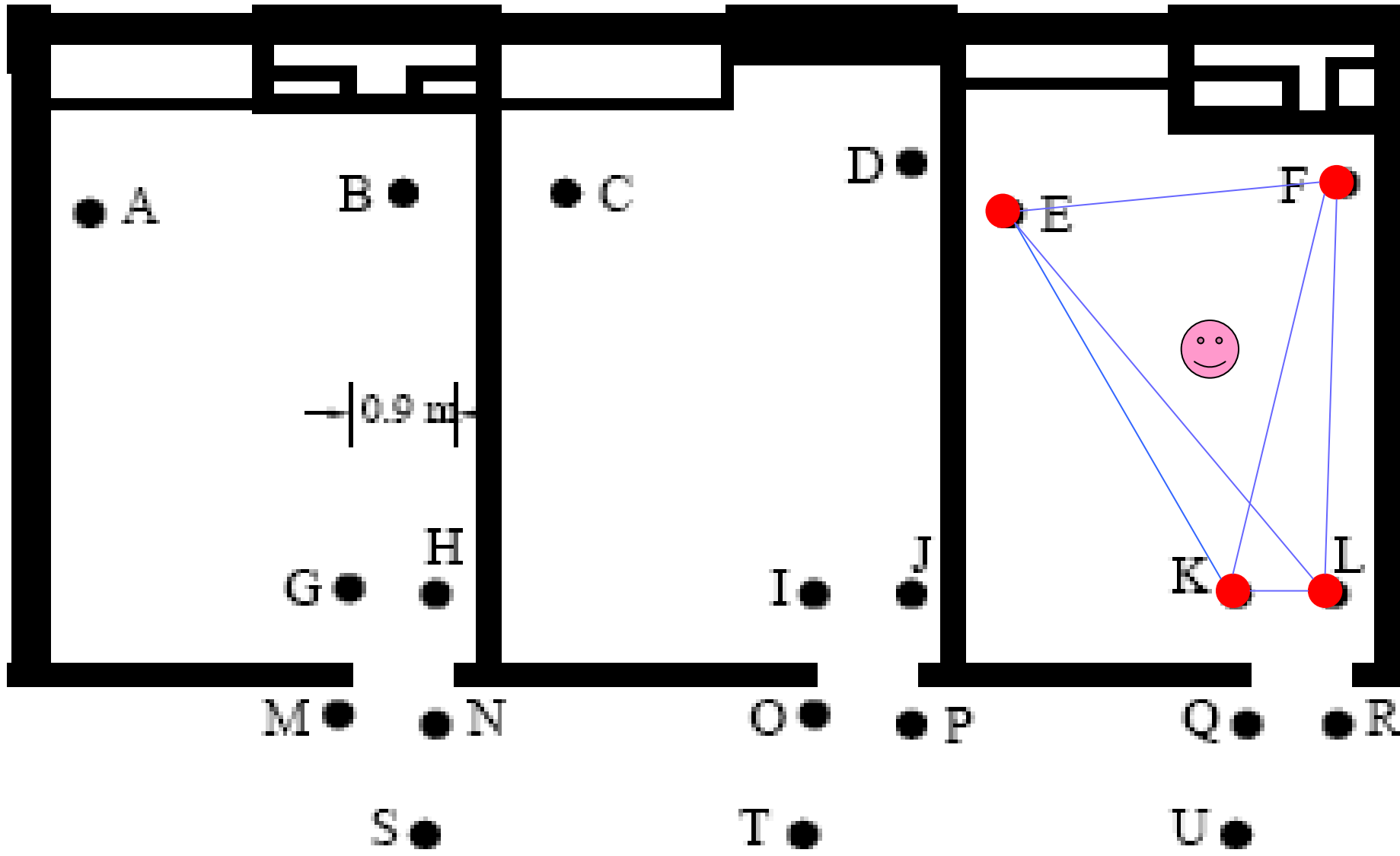
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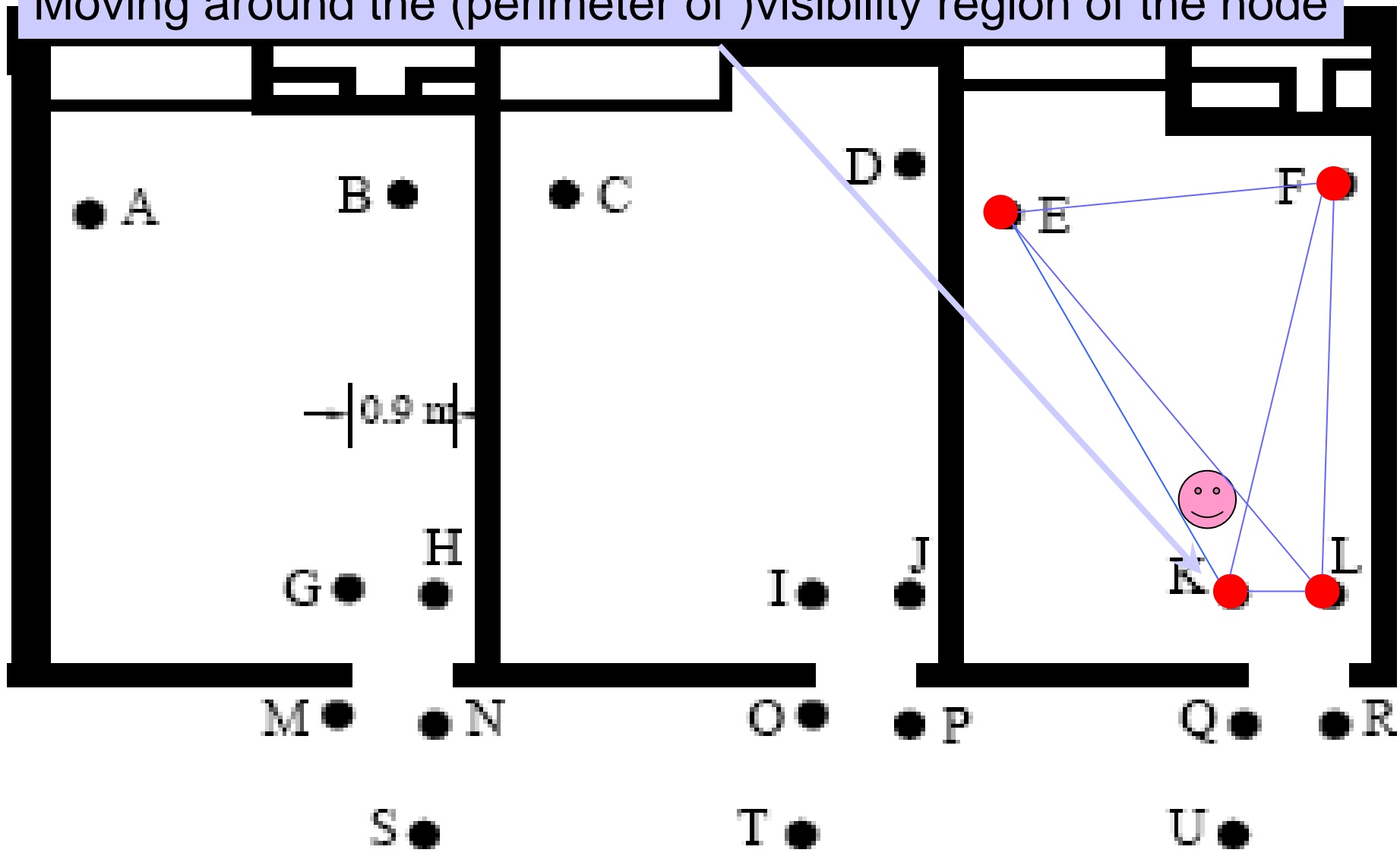


# Movement Strategy: Initialize

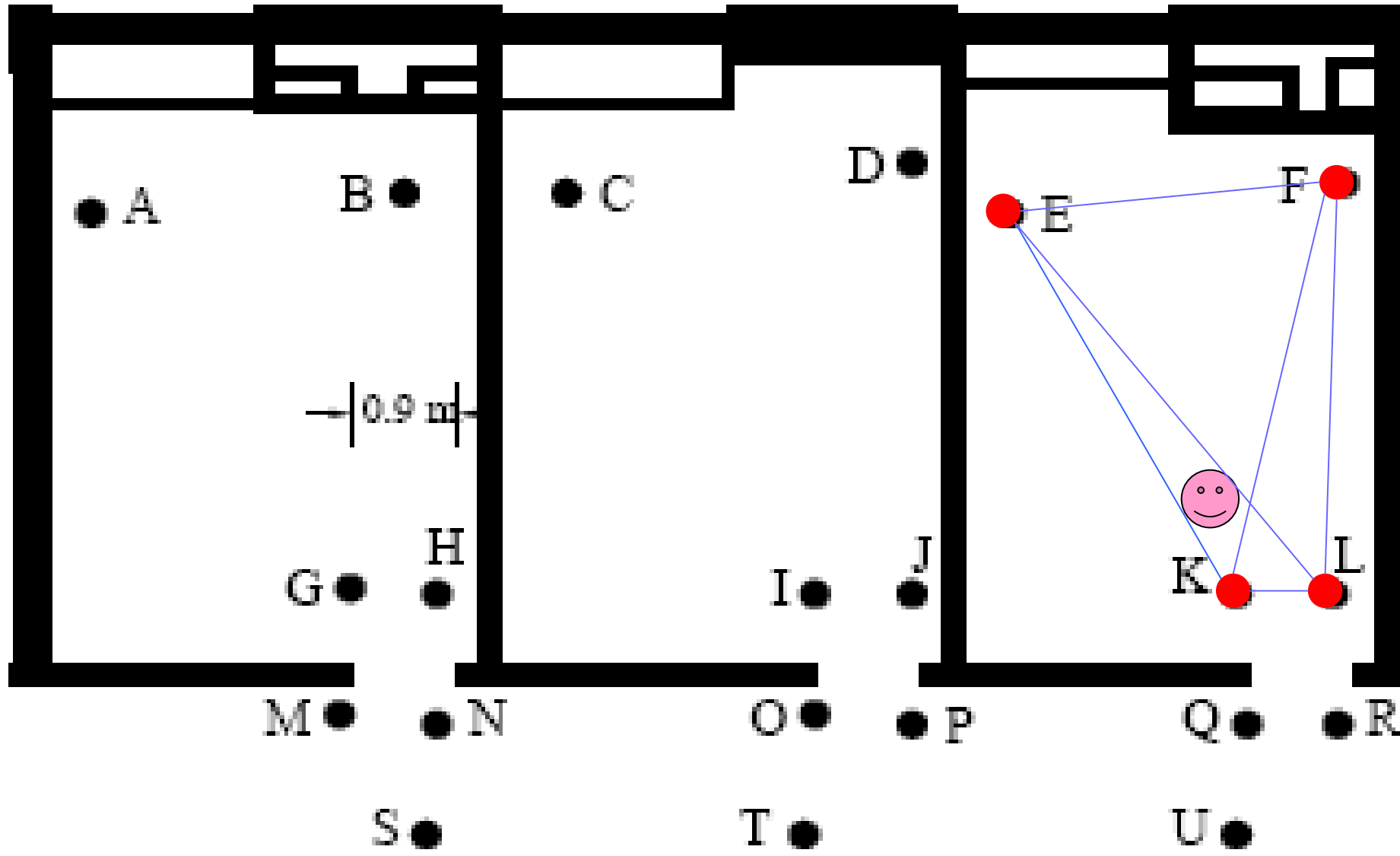


# Movement Strategy: Loop

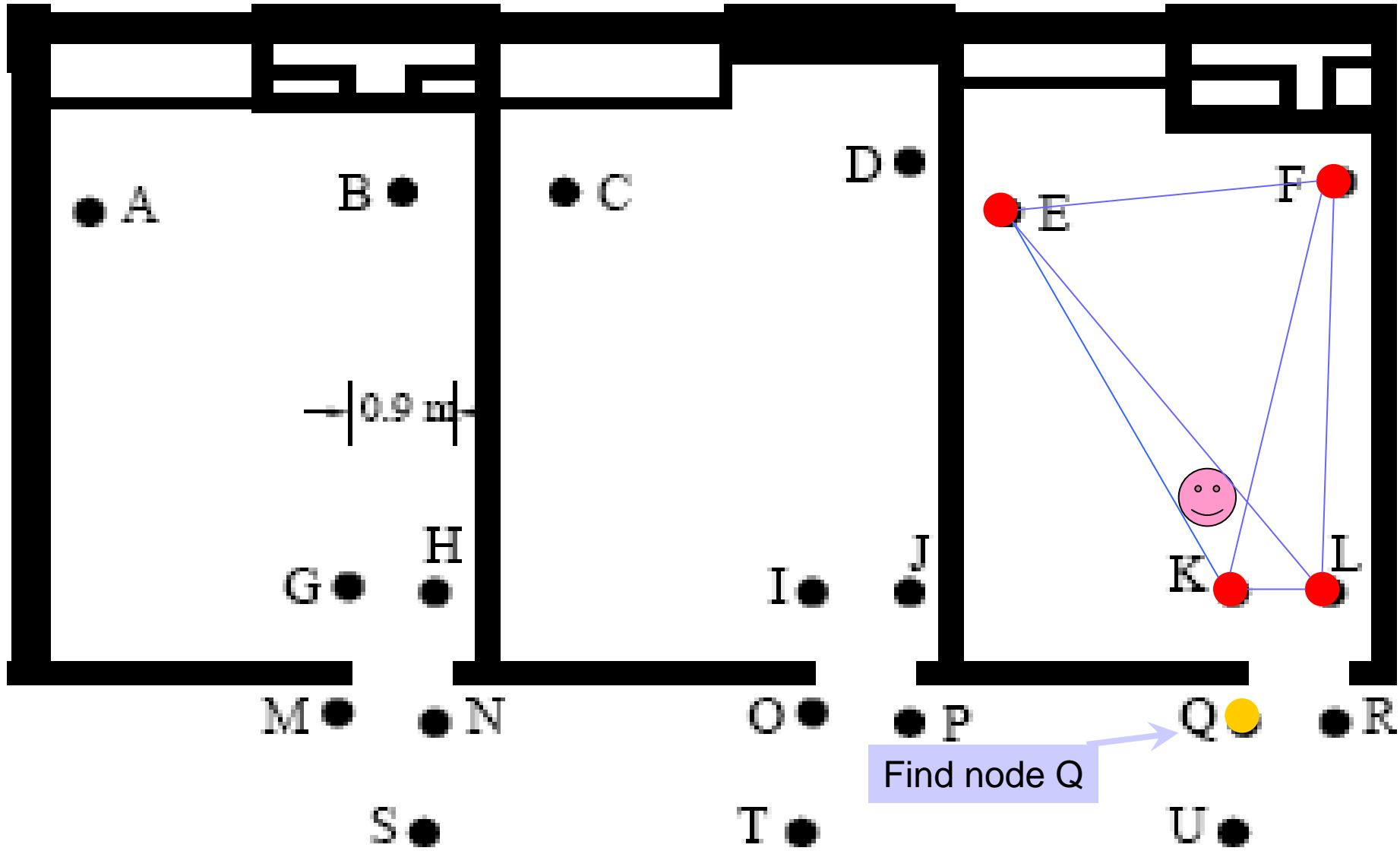
Moving around the (perimeter of) visibility region of the node



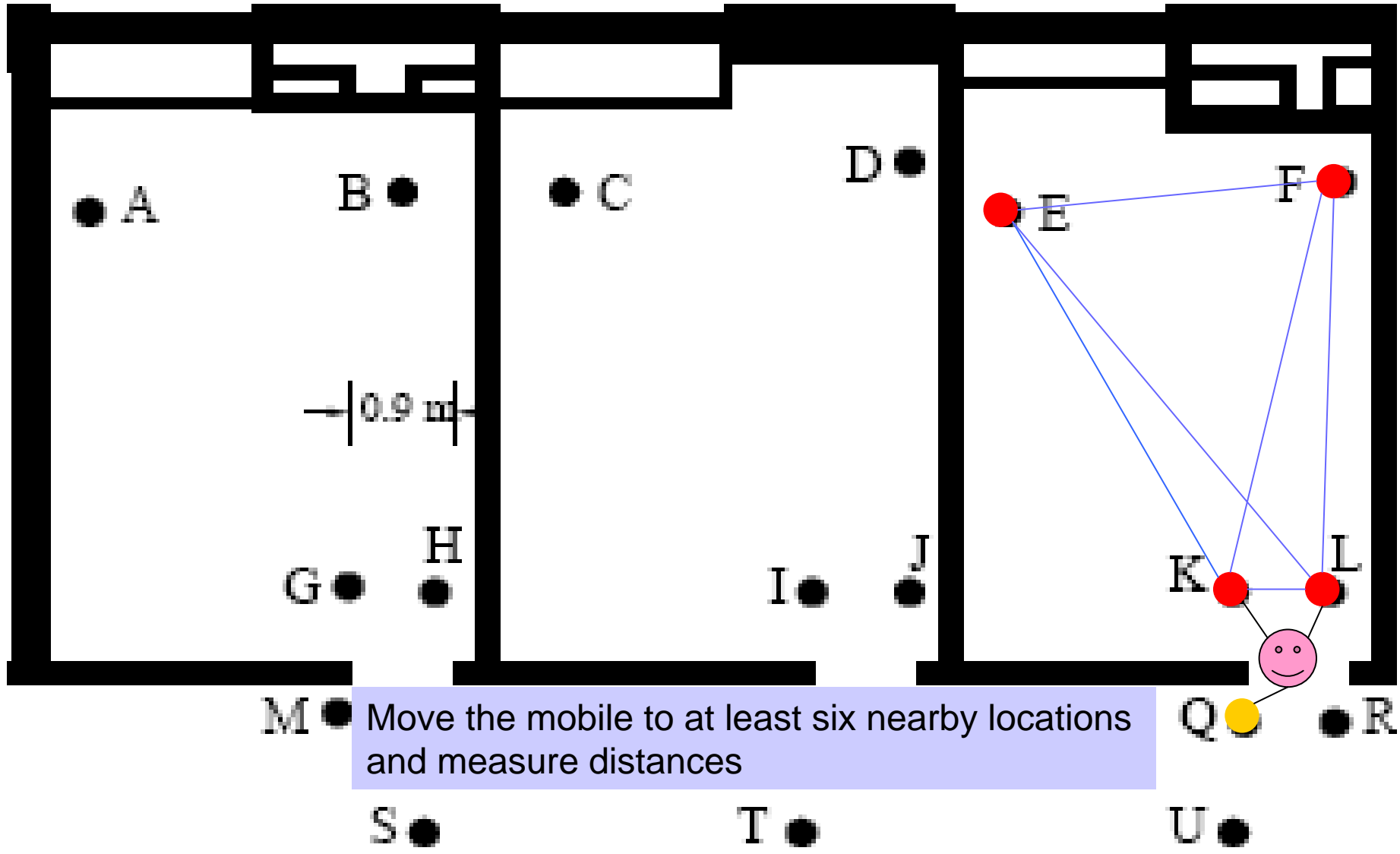
# Movement Strategy: Loop



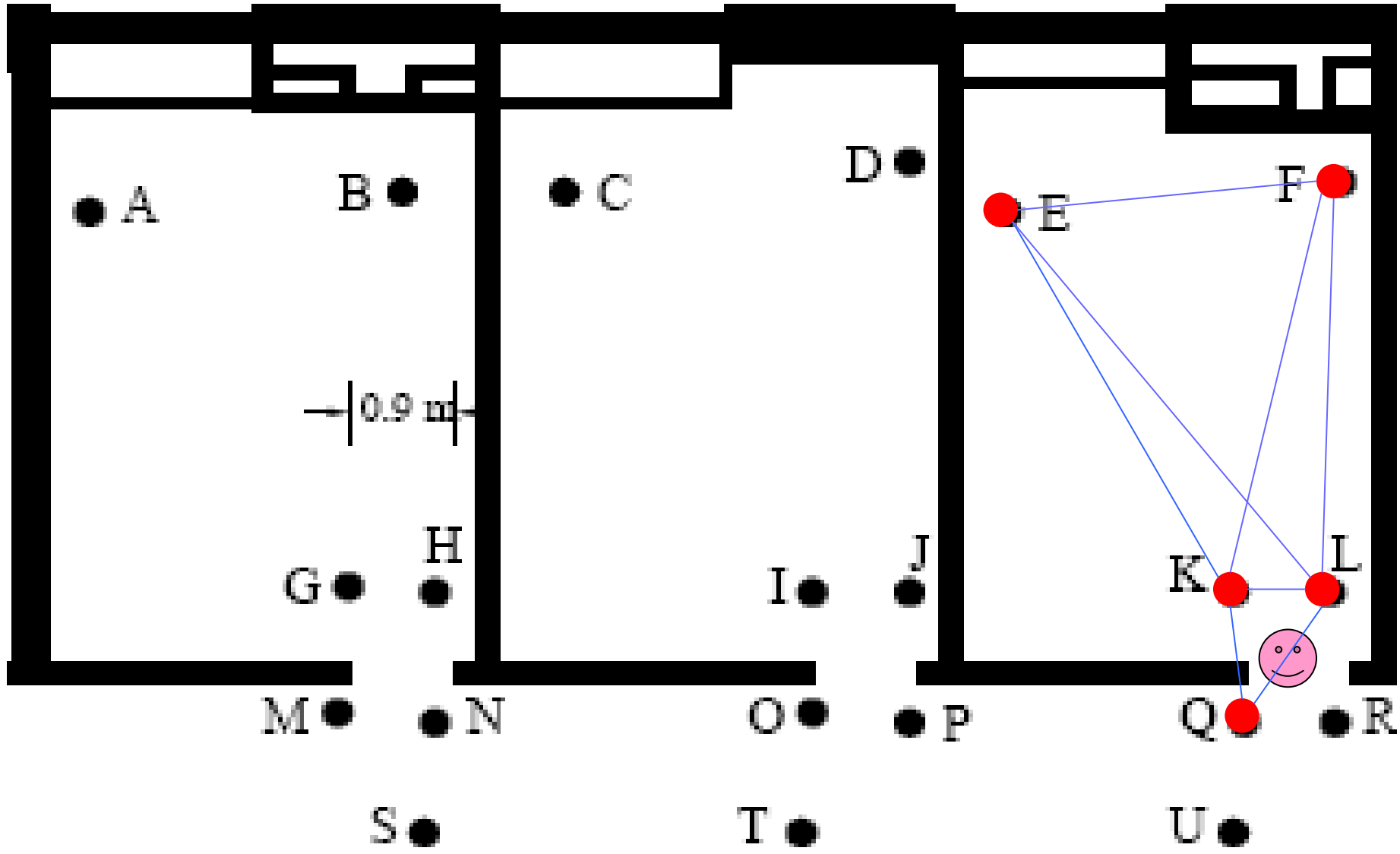
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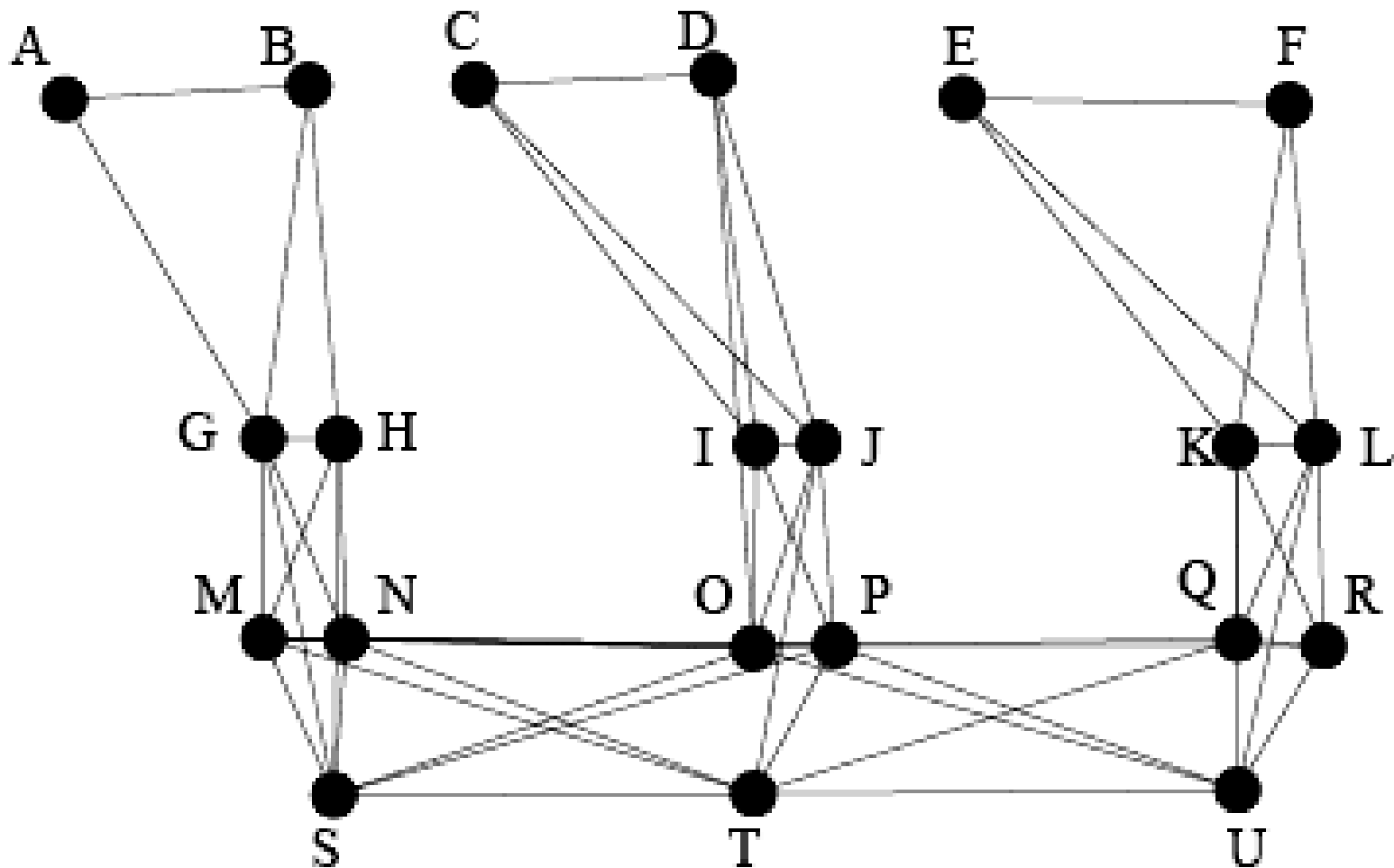


# Movement Strategy: Loop



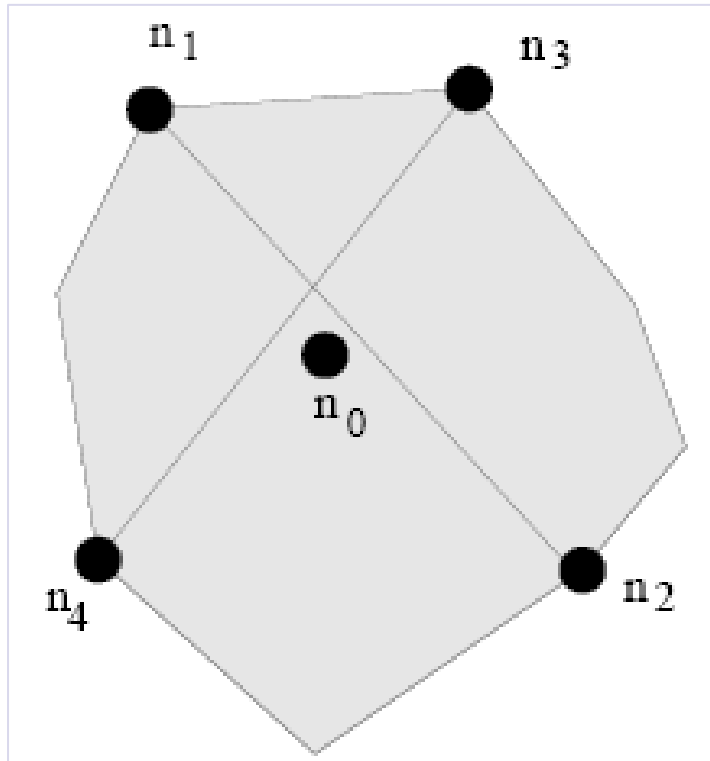


# Distance information graph



# AFL: Anchor-Free Localization

2003 April

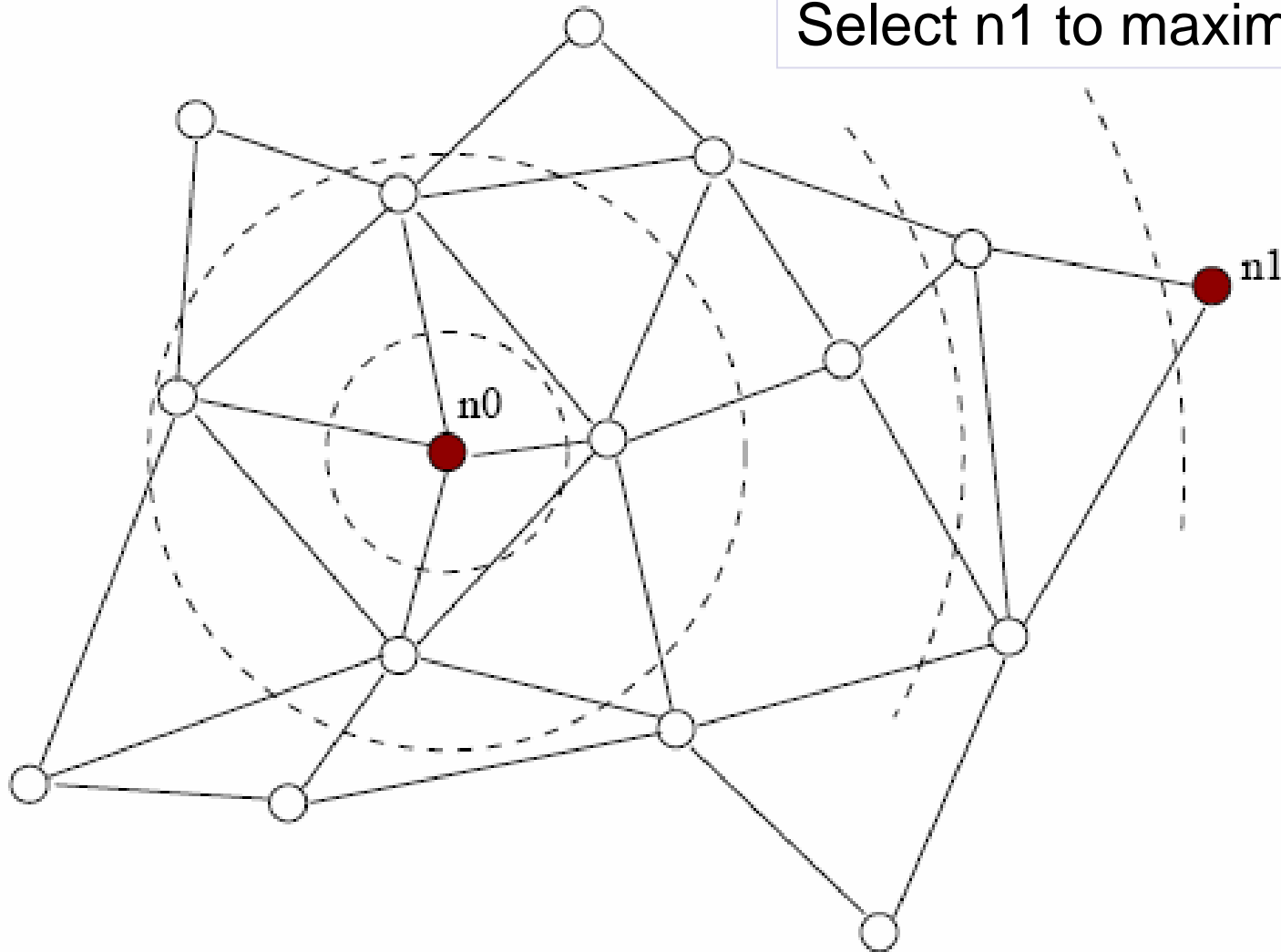


Coordinate of node  $i$

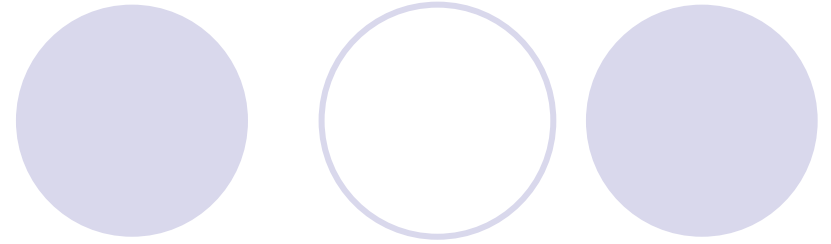
$$x(i) = Rh_{0,i} \frac{h_{3,i} - h_{4,i}}{\sqrt{(h_{3,i} - h_{4,i})^2 + (h_{1,i} - h_{2,i})^2}}$$
$$y(i) = Rh_{0,i} \frac{h_{1,i} - h_{2,i}}{\sqrt{(h_{3,i} - h_{4,i})^2 + (h_{1,i} - h_{2,i})^2}}$$

# AFL: Phase 1

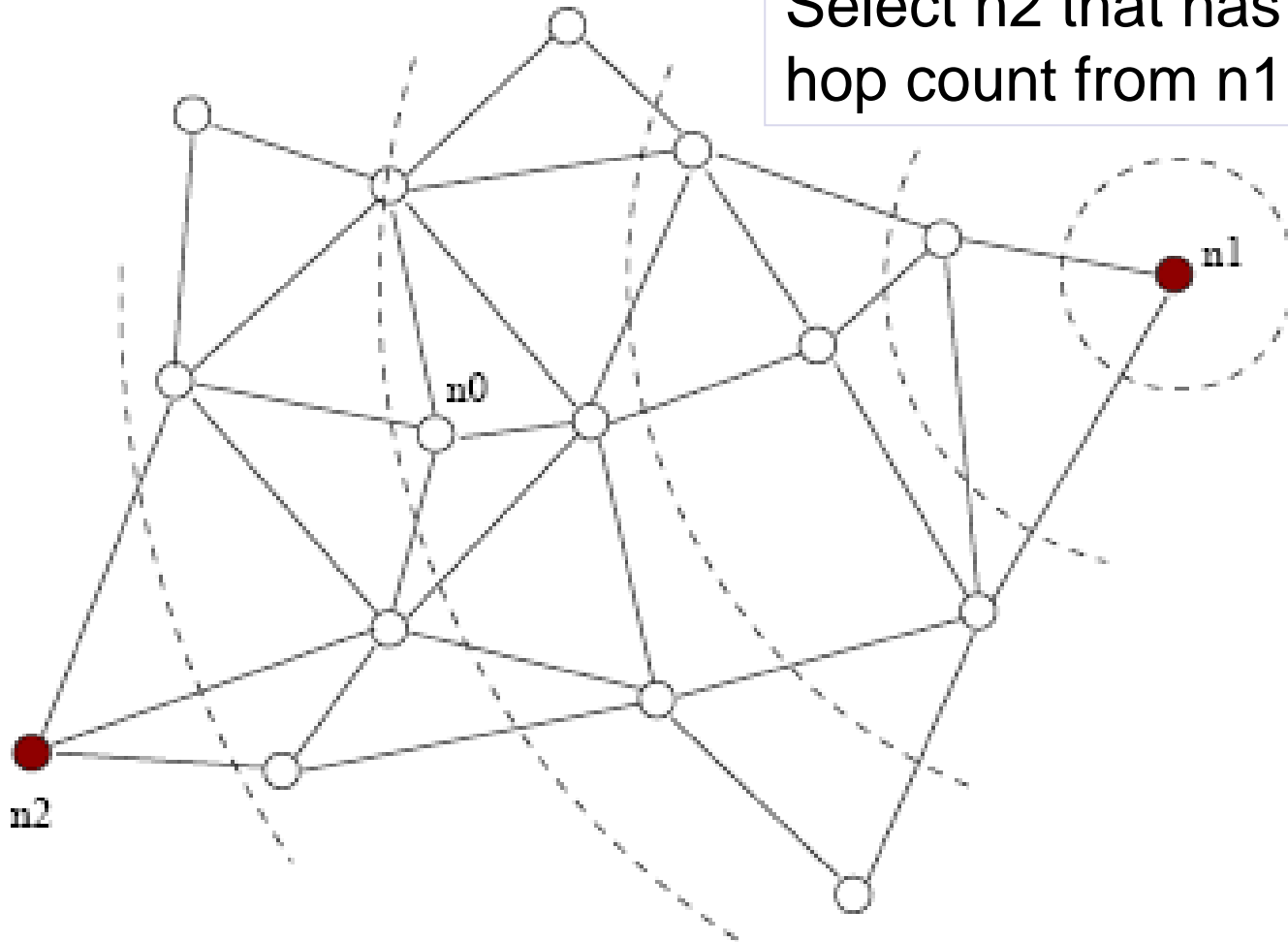
Select  $n_1$  to maximize  $h_{0,1}$



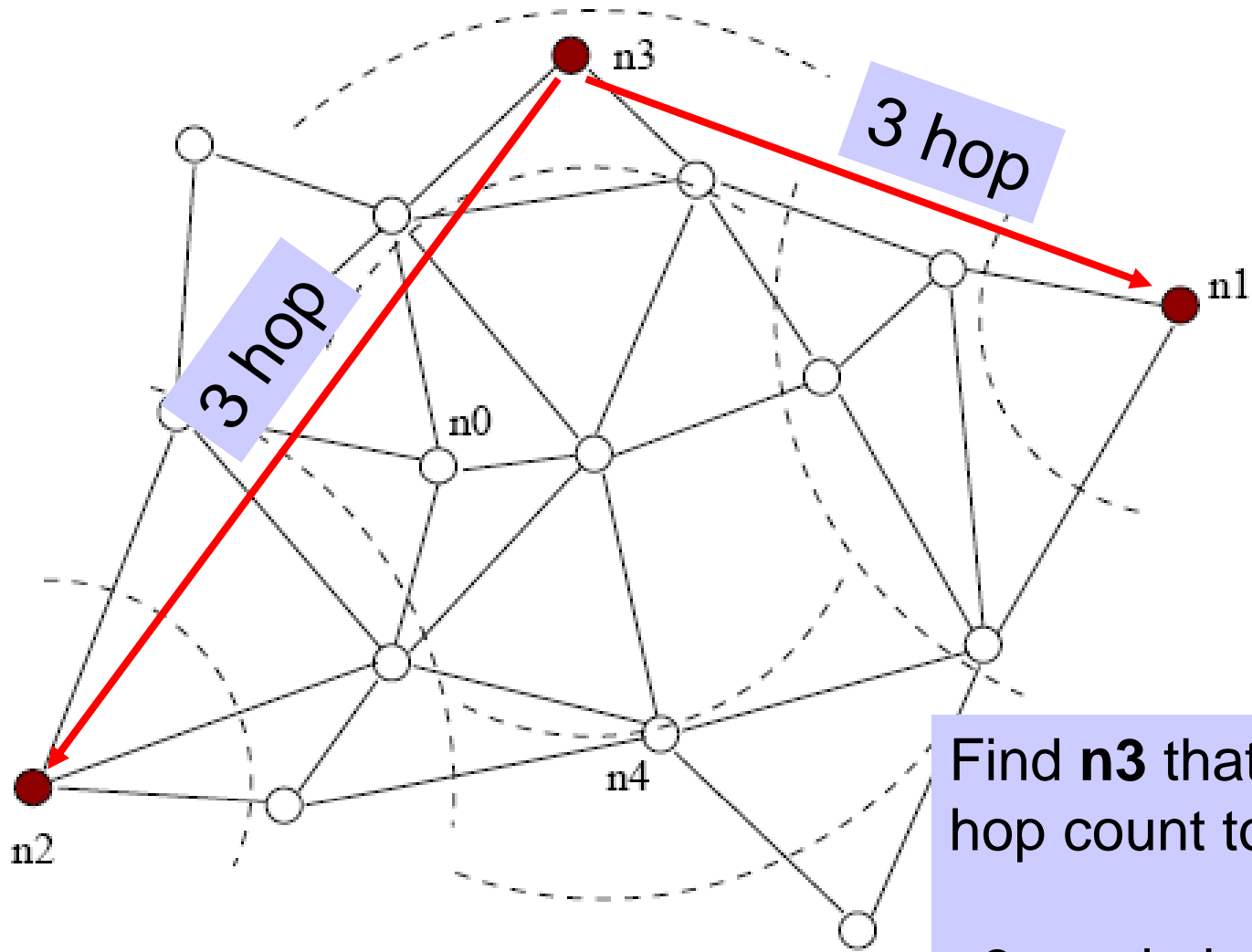
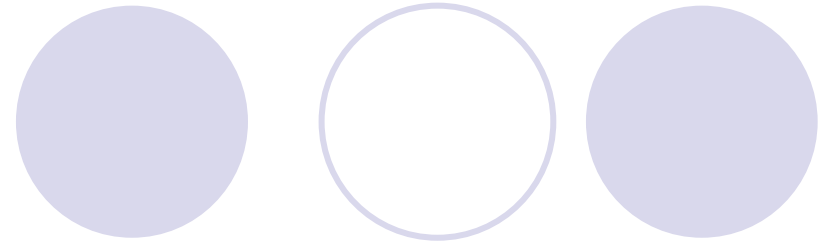
# AFL: Phase 1



Select n2 that has the maximize hop count from n1



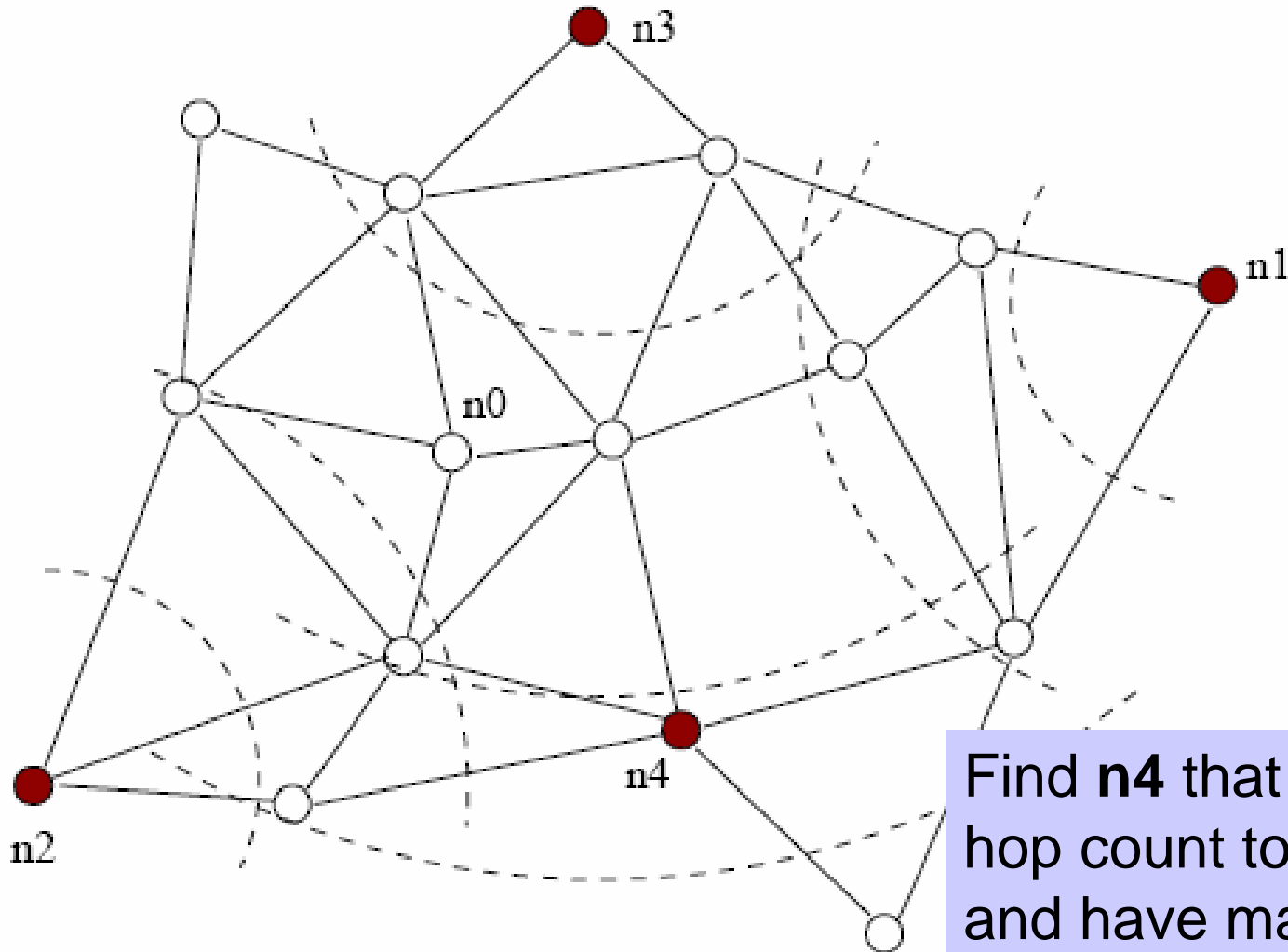
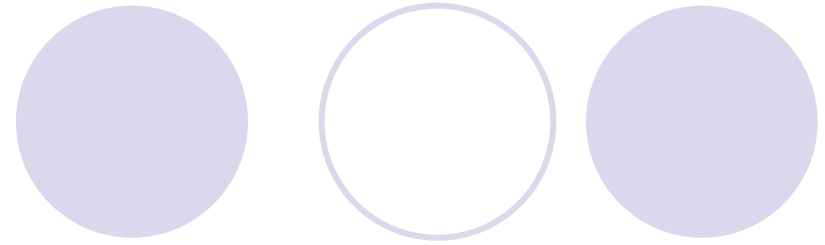
# AFL: Phase 1



Find **n3** that has the equal hop count to n1 and n2

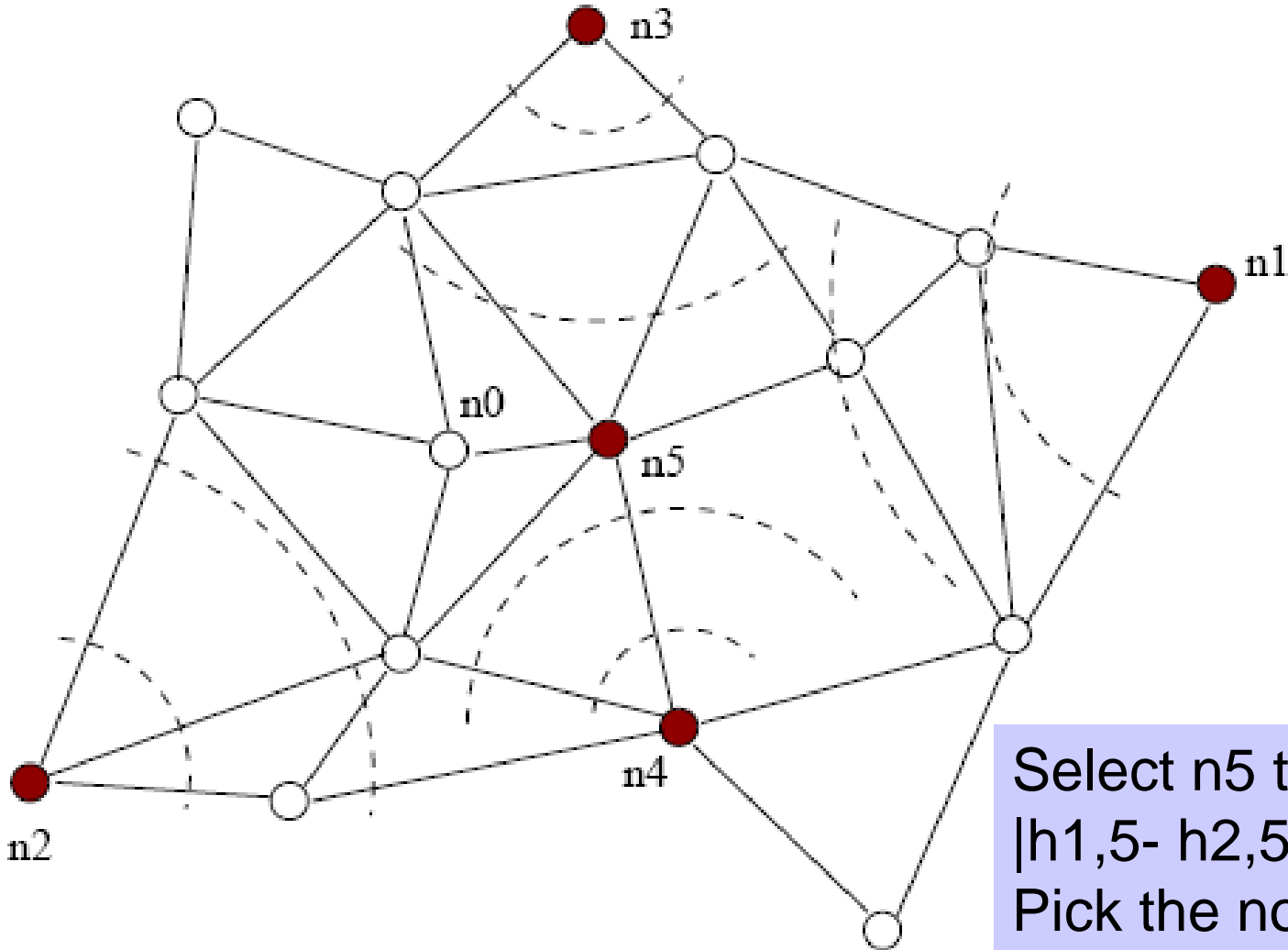
n3 maximize  $h_{1,3} + h_{2,3}$

# AFL: Phase 1



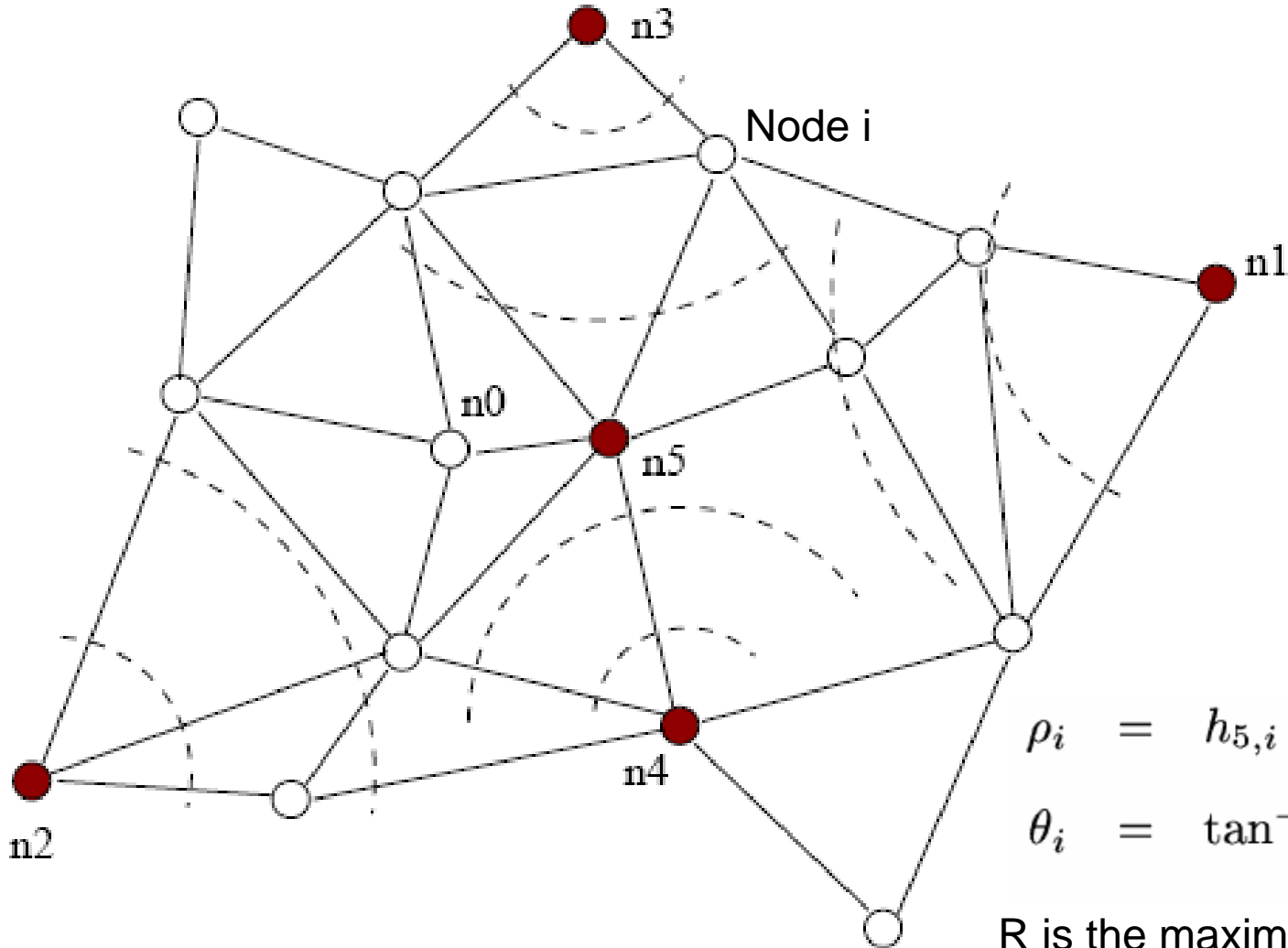
Find **n4** that has the equal hop count to n1 and n2 and have max hop count to n3

# AFL: Phase 1



Select n5 to minimize  $|h_{1,5} - h_{2,5}|$   
Pick the node that minimizes  $|h_{3,5} - h_{4,5}|$

# AFL: Phase 1

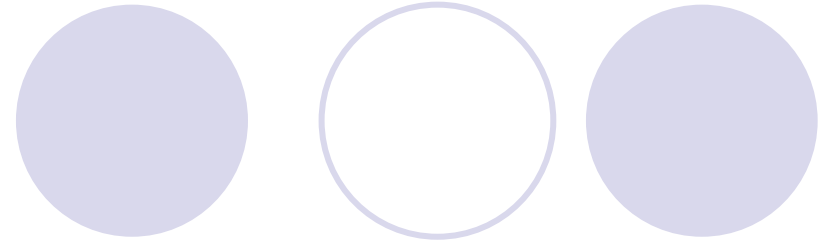


$$\rho_i = h_{5,i} \times R$$
$$\theta_i = \tan^{-1} \left( \frac{h_{1,i} - h_{2,i}}{h_{3,i} - h_{4,i}} \right)$$

R is the maximum radio range



# AFL: Phase 1

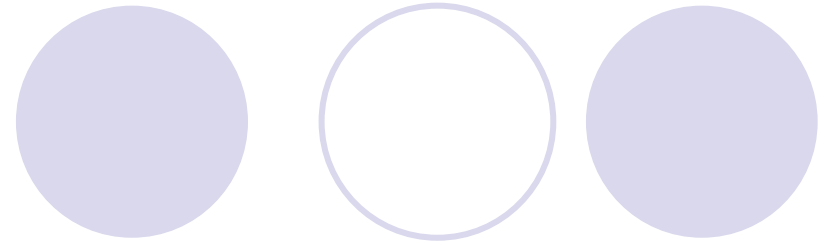


- Coordinate of node  $i$

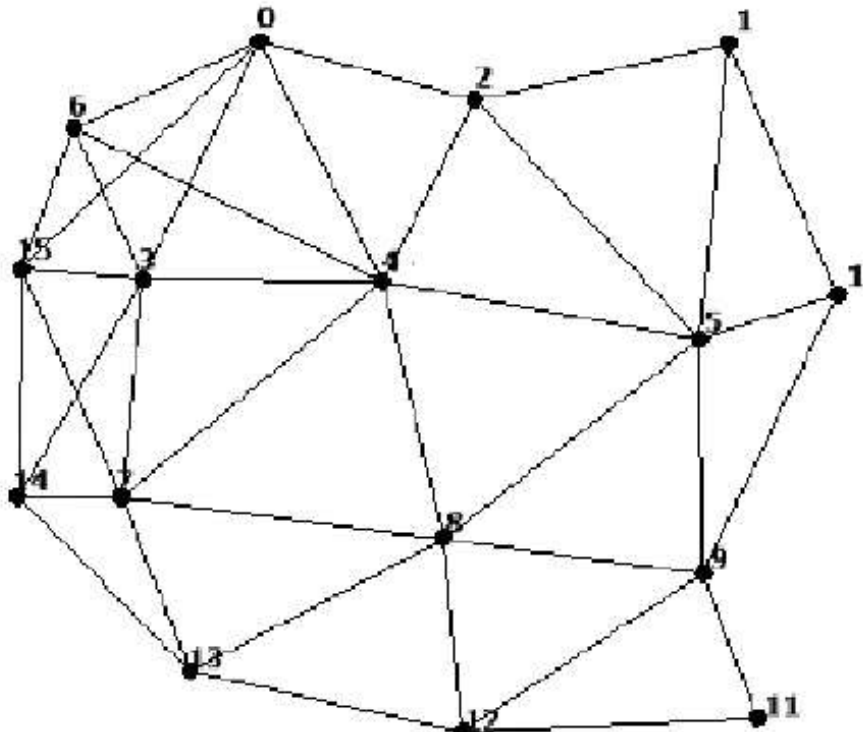
$$x(i) = Rh_{0,i} \frac{h_{3,i} - h_{4,i}}{\sqrt{(h_{3,i} - h_{4,i})^2 + (h_{1,i} - h_{2,i})^2}}$$

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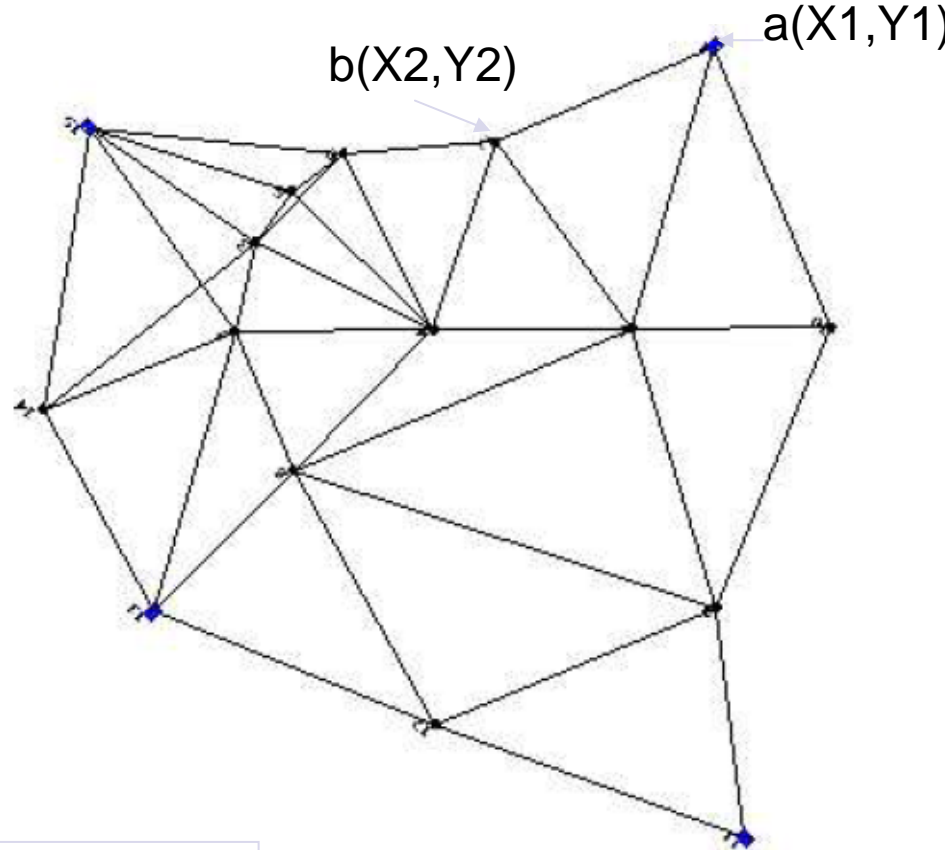
# AFL: Phase 1



True position



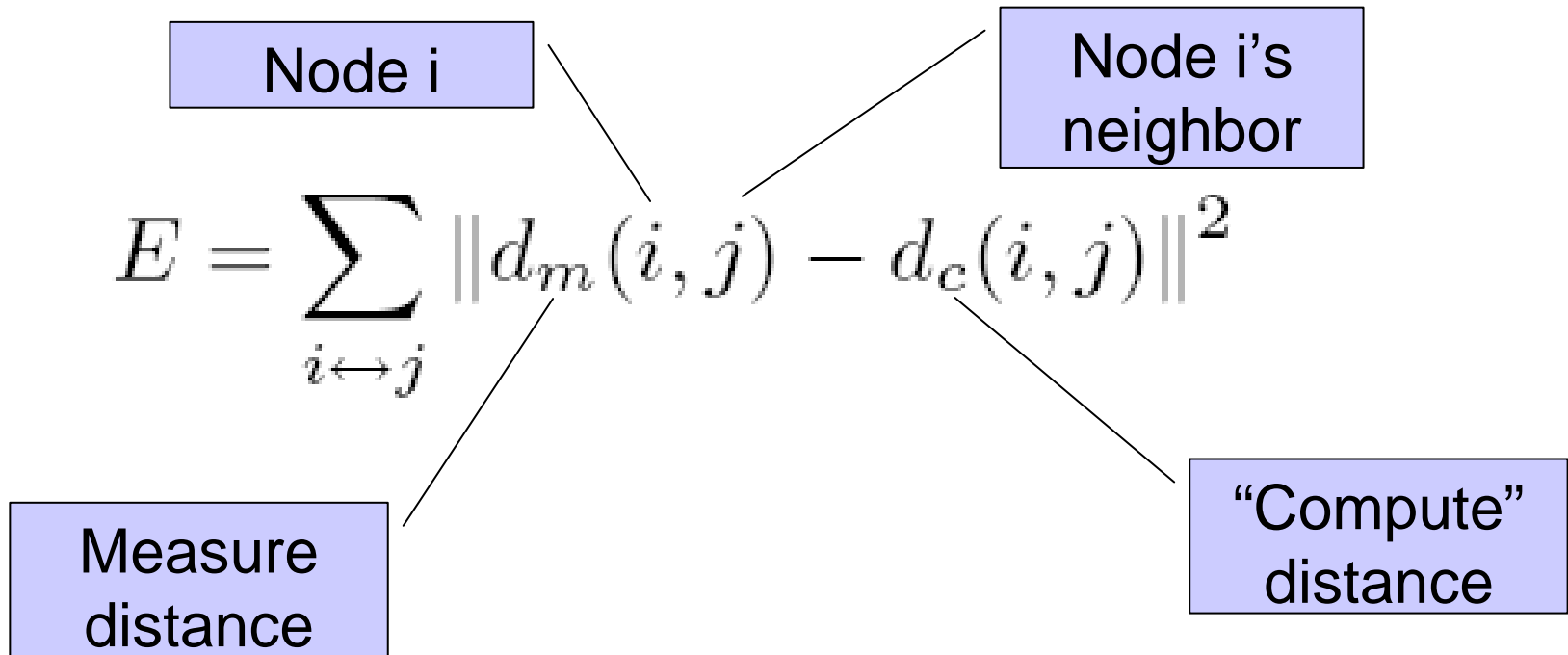
AFL Phase1



$$E_{ab} = \| d_m(a,b) - \sqrt{(X1-X1)^2 + (Y2-Y2)^2} \|^2$$

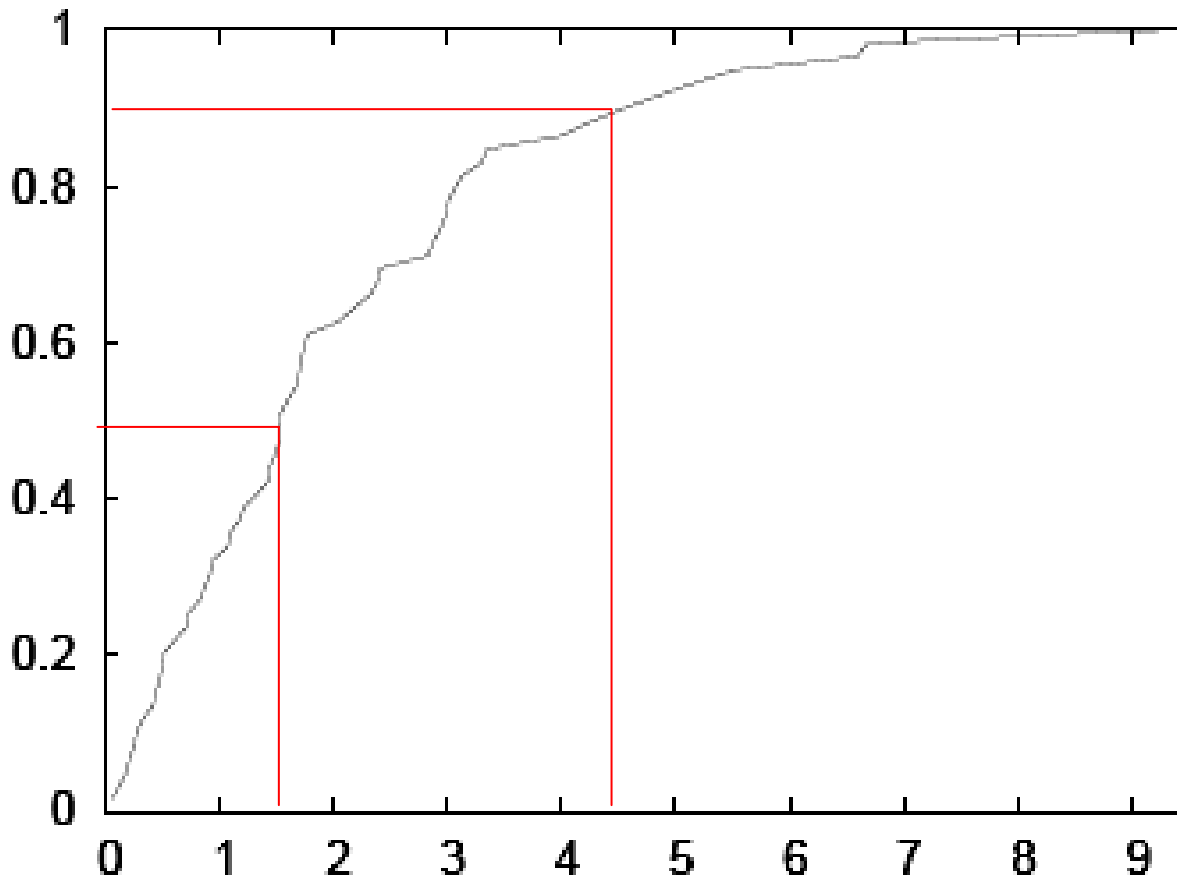
# AFL: Phase 2

- AFL use a optimization algorithm to minimize the Graph **Error**



# Performance Evaluation

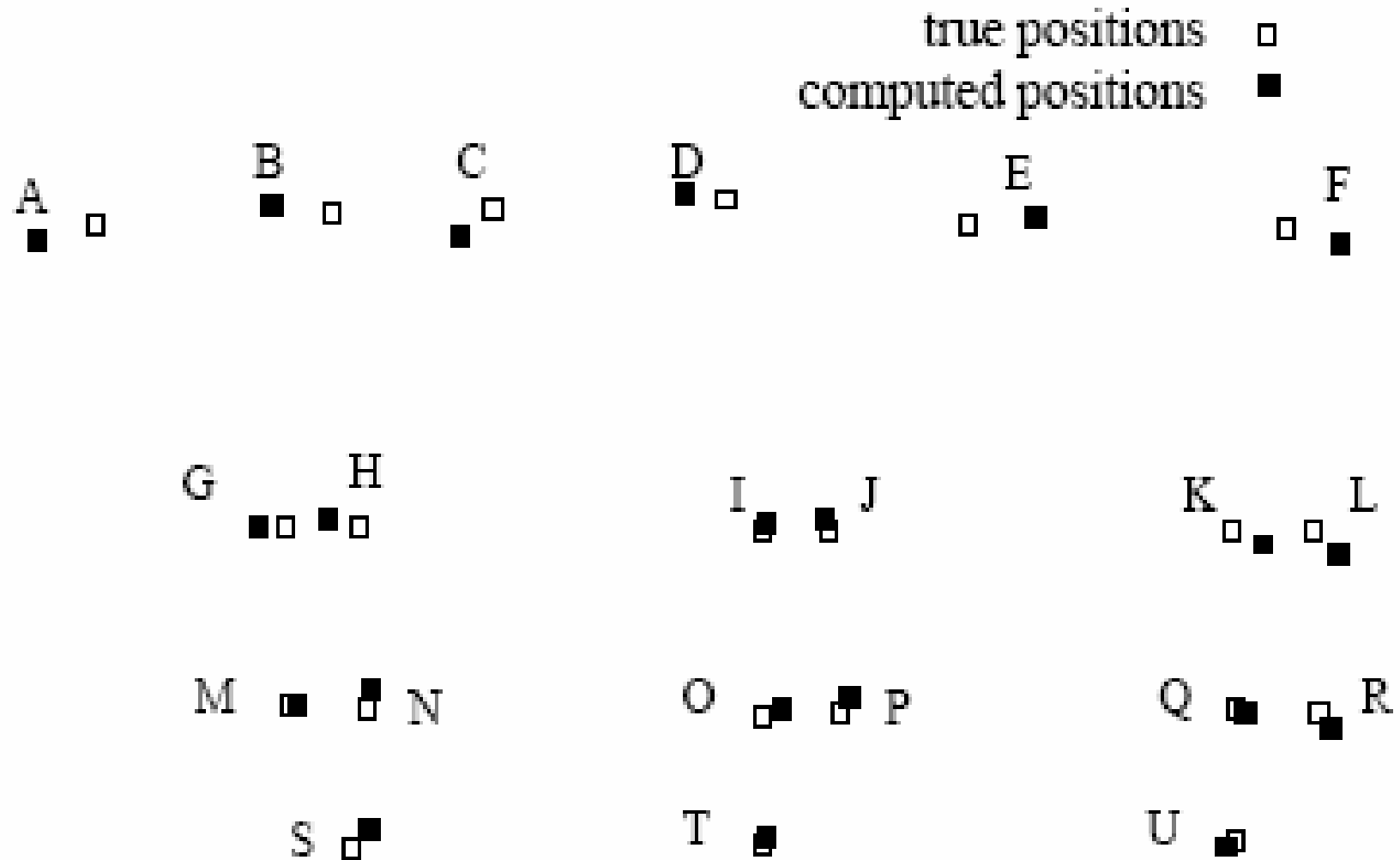
CDF of the % edge error



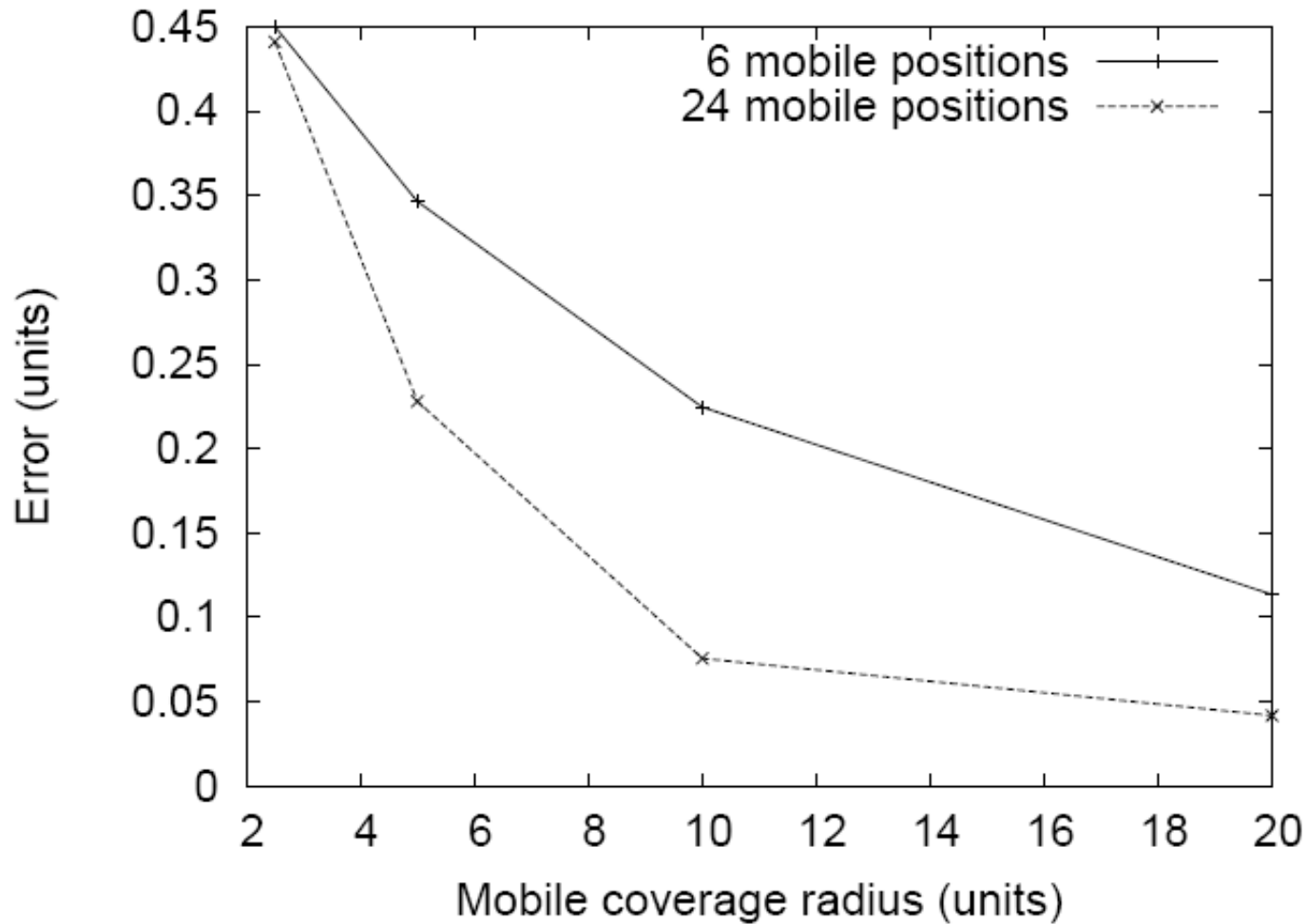
Inter-node distance estimate error %

Cause by physical obstacle such as furniture

# Coordinates obtained after running AFL

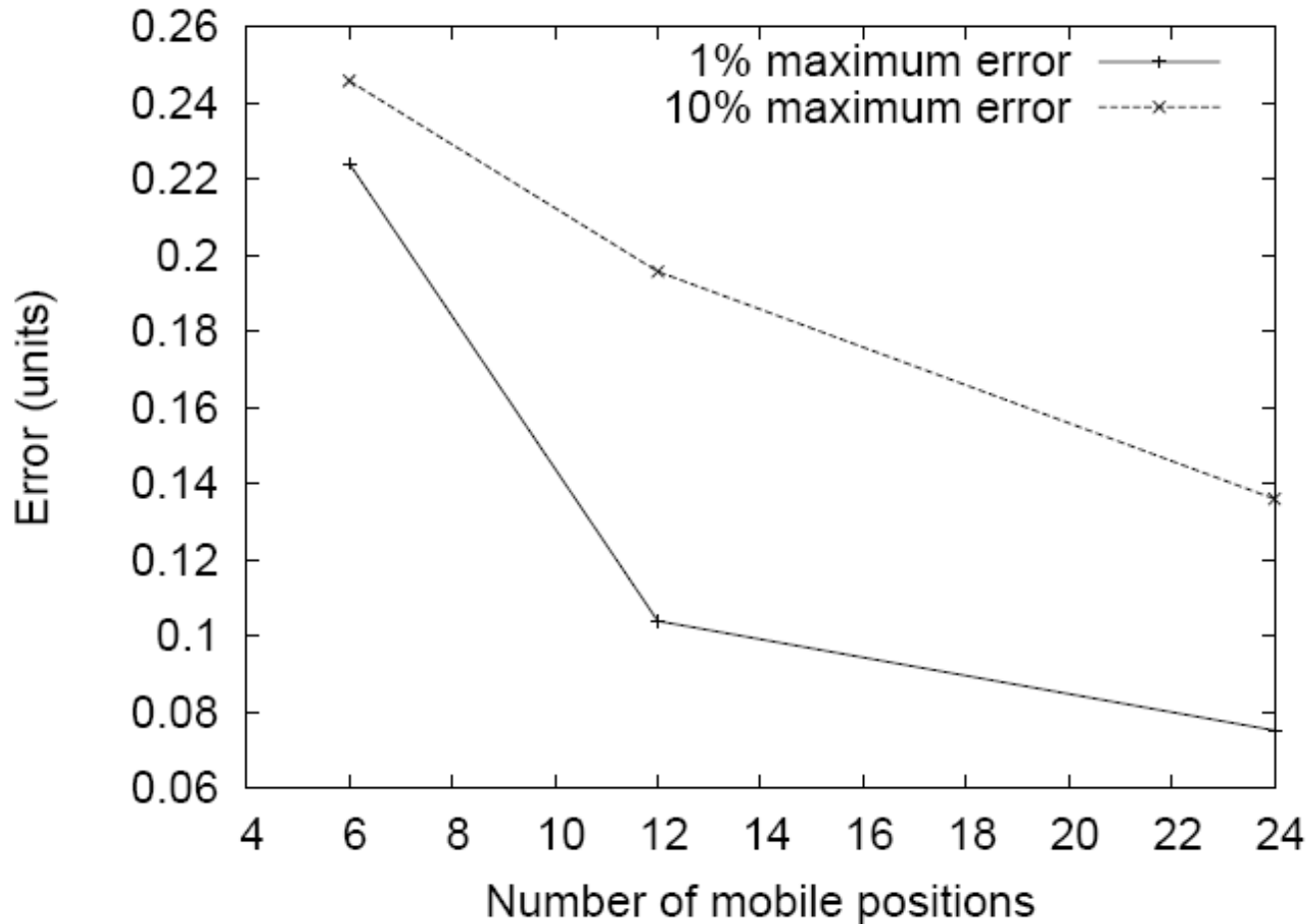


# MAL Performance



Radius larger reduce more GDOP error

# MAL Performance



Edge length error

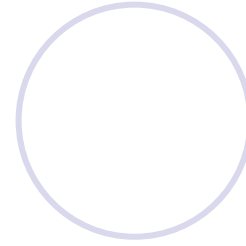
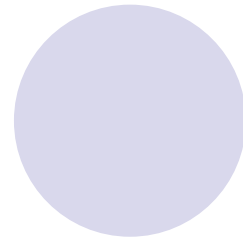
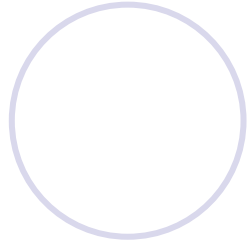
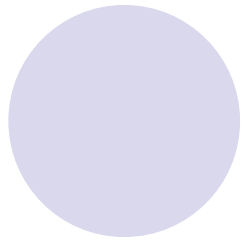
We can obtain a large number of mobile distance estimates to reduce the distance error



# Conclusion

- We evaluate the algorithm using real-world experiment
- The average distance error is less than 1.5%
- With sufficient distance samples, AFL can produce coordinate assignment





THANK YOU