

A Distributed Policy Scheduling for Wireless Sensor Networks

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Outline

- Introduction
- Coloring
- Color scheduling scheme
- Simulation
- Conclusion

Introduction

- Save energy by collision avoidance + duty cycling
- Although duty cycling can save power, it also disrupts network performance
 - Link disconnections
- Duty cycling needs synchronization to solve the above problems

Introduction(2)

- Save energy by integrating two tasks, collision avoidance and duty cycles, into one scheduling of sensors' activities
- This scheme consists of two parts:
 - *A coloring scheme*
 - *A color scheduling scheme*
- To reduce packet latency and save energy, guarantee the communication connectivity of links only in a sparse connected subgraph

Coloring

- Traditional coloring: $L(d,k)$
 - A function that assigns to each node an integer such that if x and y are adjacent, then $|color(x) - color(y)| \geq d$
; if there is a two-edge path, then $|color(x) - color(y)| \geq k$
 - To guarantee an entirely collision-free schedule in WSN
- In this paper, reduce the number of required colors

Why $L_s(d,k)$?

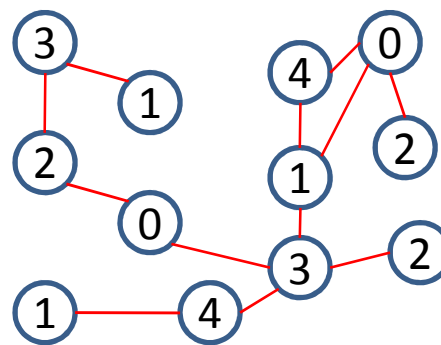
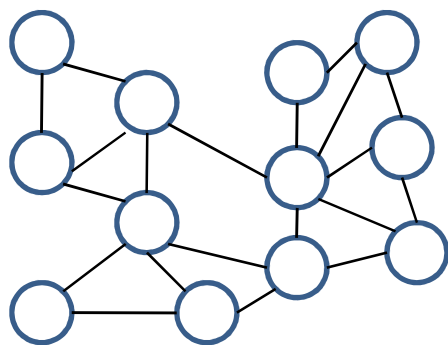
- As colors represent resources in networks, e.g. time slots in TDMA and codes in CDMA, due to high node density or constrained system resources.
- Communication among all pairs of nodes only requires collision-free links forming strongly connected graph
- Data gathering only requires that each node is connected to the sink by a collision-free path

$$L_s(d,k)$$

- We don't need to consider the entire graph, just consider its subgraph
- [21]: relative neighborhood graphs; [22]: local minimal spanning trees
- Network topologies can be changed by adjusting nodes' transmission power and the number of colors can be reduced by only guaranteeing required connectivity

$L_S(d,k)$ -coloring (1)

$$|color(x) - color(y)| \geq \begin{cases} d & \text{if } y \in N_S^+(x) \\ k & \text{if } \exists z \in N_S^+(x), y \in N_G(z) \end{cases}$$



index	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
T[20]=	3	0	0	1	1	3	3	4	4	1	1	2	2	4	4	0	0	2	2	3
R[20]=	0	3	1	0	3	1	4	3	1	4	2	1	4	2	0	4	2	0	3	2

$L_S(d,k)$ -coloring (2)

$$\begin{aligned}
 N_{S,G}(x) &\equiv N_S^+(x) \cup \{y \mid \exists z \in N_S^+(x), y \in N_G(z)\} \\
 D_{S,G}(x) &\equiv N_{S,G}(x) \cup \{y \mid x \in N_{S,G}(y)\} \\
 &= N_S^+(x) \cup \{y \mid \exists z \in N_S^+(x), y \in N_G(z)\} \cup \\
 &\quad N_S^-(x) \cup \{y \mid \exists z \in N_G(x), y \in N_S^-(z)\}
 \end{aligned}$$

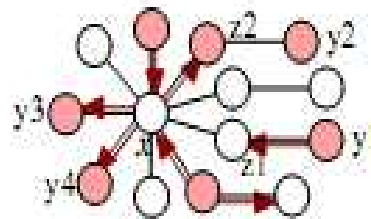


Fig. 2. Example of $N_{S,G}(x)$ and $D_{S,G}(x)$

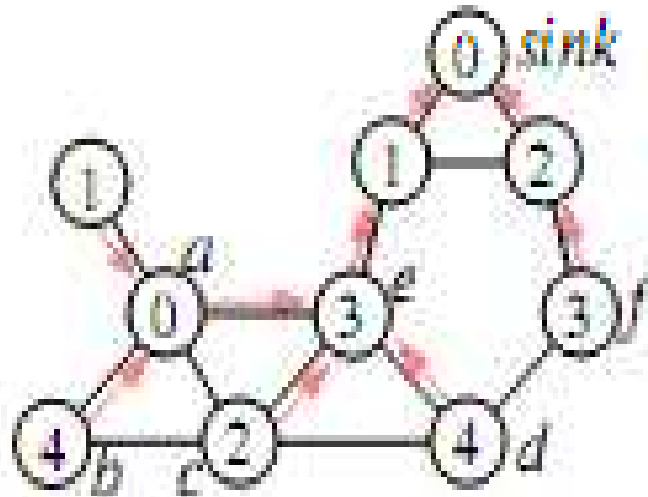
$L_s(1,1)$ -coloring

$$\text{wait}_x \equiv \{z \mid z \in D_{S,G}(x) \wedge (\text{priority}(z) > \text{priority}(x))\}$$

- Distributed algorithm
- On node x :
 - when received y 's message $\langle y, \text{color}(y) \rangle$
 - If $y \in N_G(x)$, it broadcasts it
 - If $y \in \text{wait}(x)$, remove y from $\text{wait}(x)$, and record $\text{color}(y)$
 - Until $\text{wait}(x)$ is empty, it chooses the smallest color from remaining colors, then broadcasts itself

$L_T(1,1)$ -coloring

- Data gathering from nodes to sink
- In BFS order



Color scheduling (1)

- Nodes are scheduled in (T,R) ; in slot i , a node is allowed to transmit iff its color is $T[i\%F]$, otherwise it turns off its radio to sleep
- To guarantee the connectivity of a link $\langle a,b \rangle \in S$ (fully connected schedule)

$$\begin{array}{l} T = 0 \ 0 \ \dots \ 0 \ 1 \ 1 \ \dots \ 1 \ \dots \ K-1 \ K-1 \ \dots \ K-1 \\ R = 1 \ 2 \ \dots \ K-1 \ 0 \ 2 \ \dots \ 1 \ \dots \ 0 \ 1 \ \dots \ K-2 \end{array}$$

Color scheduling (2)

- To reduce the number of switching between sleep and active modes
- The following scheme is optimal:

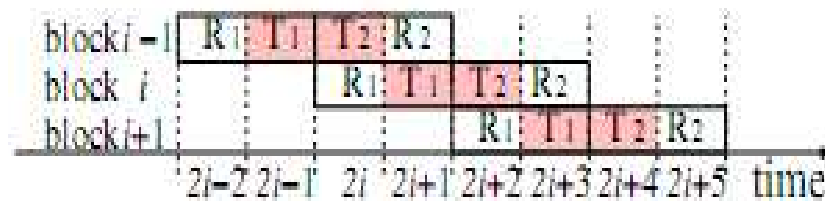


Fig. 10. Organize slots into blocks

Color scheduling (3)

- Block i is assigned to color $\sigma[i \% |\sigma|]$

$$\forall k \in [0, |\sigma| - 1], R[2k] = T[2k + 1] = T[(2k + 2) \% 2 |\sigma|] = R[(2k + 3) \% 2 |\sigma|] = \sigma[k]$$

- If $\exists k, (\sigma[k] = x \wedge \sigma[k+1] = y)$ or $(\sigma[k] = y \wedge \sigma[k+1] = x)$, then the schedule is fully connected.
- Hence, the main work is to construct σ

Color scheduling (4)

if $K = 4p + 1, p > 0$ **then**
 $\forall r \in [1, p], \beta(K, r, 2p + 1 - r)$ is constructed.
else if $K = 4p + 3, p > 0$ **then**
 $\forall r \in [1, p], \beta(K, r, 2p + 1 - r)$ is constructed.
 $\alpha(K, 2p + 1)$ is constructed.
endif
 σ is a concatenate of all the constructed sequences.

Example of σ construction

$$\begin{aligned}\alpha(K, d) &\equiv 0, d, 2d, \dots, (K-1)d \\ \beta(K, d_1, d_2) &\equiv 0, d_1, d_1+d_2, (d_1+d_2)+d_1, 2(d_1+d_2), 2(d_1+d_2)+d_1, \\ &\dots, (K-1)(d_1+d_2), (K-1)(d_1+d_2)+d_1\end{aligned}$$

$K = 9$: $\sigma = \beta(9, 1, 4) \circ \beta(9, 2, 3)$, where

$$\beta(9, 1, 4) = 0, 1, 5, 6, 1, 2, 6, 7, 2, 3, 7, 8, 3, 4, 8, 0, 4, 5$$

$$\beta(9, 2, 3) = 0, 2, 5, 7, 1, 3, 6, 8, 2, 4, 7, 0, 3, 5, 8, 1, 4, 6$$

$K = 11$: $\sigma = \beta(11, 1, 4) \circ \beta(11, 2, 3) \circ \alpha(11, 5)$, where

$$\beta(11, 1, 4) = 0, 1, 5, 6, 10, 0, 4, 5, 9, 10, 3, 4, 8, 9, 2, 3, 7, 8, 1, 2, 6, 7$$

$$\beta(11, 2, 3) = 0, 2, 5, 7, 10, 1, 4, 6, 9, 0, 3, 5, 8, 10, 2, 4, 7, 9, 1, 3, 6, 8$$

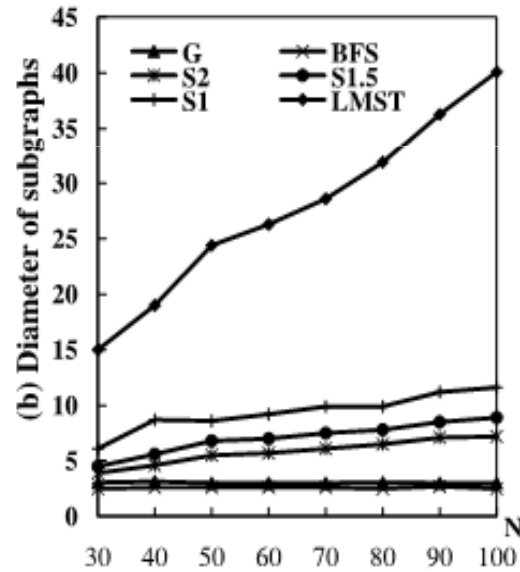
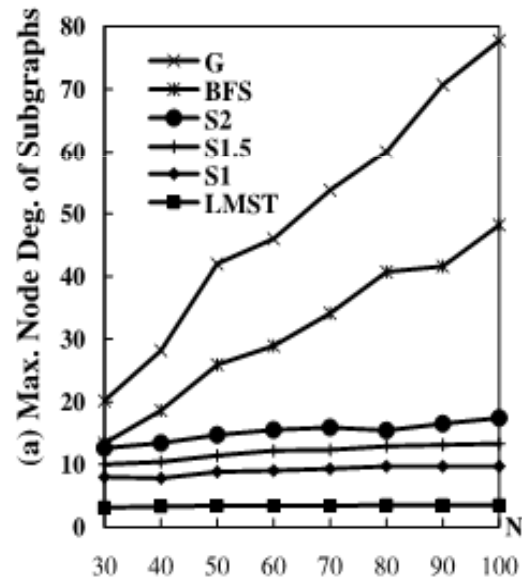
$$\alpha(11, 5) = 0, 5, 10, 4, 9, 3, 8, 2, 7, 1, 6$$

Simulation(1)

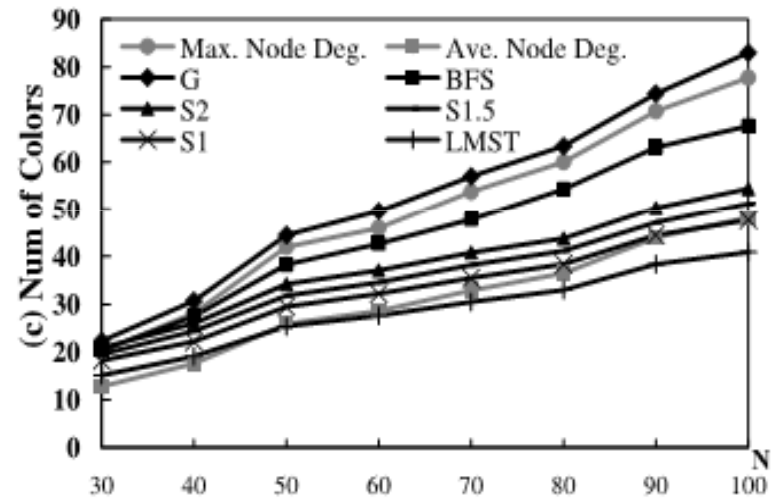
- Consider 4 levels of connectivity

Connectivity	Subgraph S	Denotation
Full Reserved	G	G
Strong Connectivity	LMST	LMST
Strong Connectivity w.h.p.	$\mathcal{G}_{n,d \log n,R}, d = 1, 1.5, 2$	$S1, S1.5, S2$
Connectivity to Sink	BFS rooted at sink	BFS

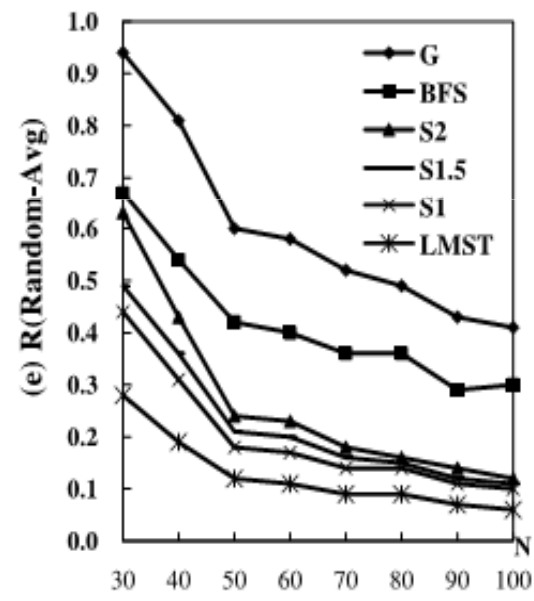
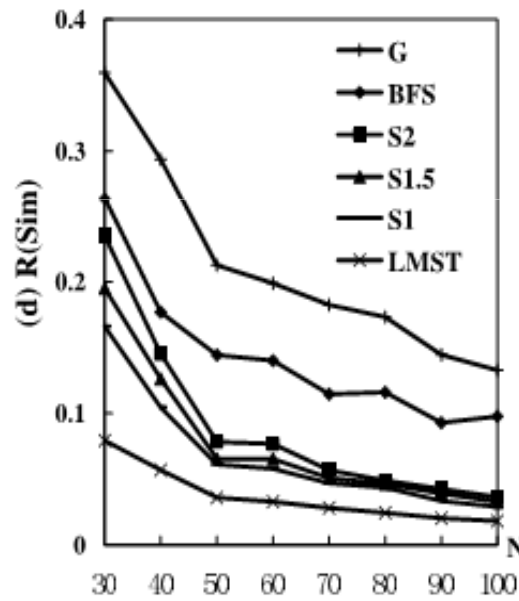
Simulation(2)



Simulation(3)



Simulation(4)



Conclusion

- According to the simulation, if this coloring is used by collision avoidance scheme
 - much less colors than traditional colorings
 - much less packet latency than traditional colorings